

PRESSURE BASED INCOMPRESSIBLE SOLVER IN SU2

SU2 Developers meet 2019 | Koodly Ravishankara, A. (Akshay)



ECN

TNO

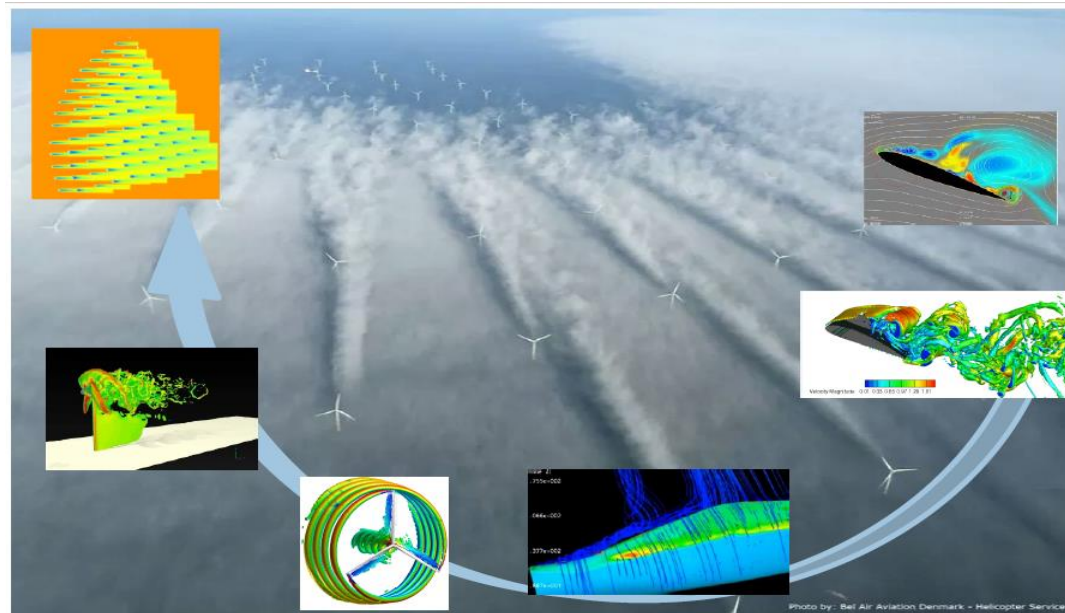
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CONTENTS

- › Wind energy at ECN part of TNO
- › Incompressible flow equations
- › Pressure-based system in SU2
- › Implementation details and challenges
- › Test Cases
- › Upcoming work

WIND ENERGY AT ECN PART OF TNO

- › Research on many topics of **renewable energy technologies** – Wind energy, Solar energy, Biomass, etc.
- › Wind energy unit mainly focused on **low-fidelity tools** that are tailor made for wind energy applications (about 50 researchers on various topics)
- › **SU2** is our first serious attempt to include **CFD** in our research/design tool chain



INCOMPRESSIBLE FLOW METHODS

- › Main difficulty – Pressure velocity coupling.
- › *Compressible flows* – Solve for density in the continuity equation and use equation of state for pressure.
- › *Incompressible flows* – Continuity equation reduces to divergence condition and no governing equation for pressure.
- › **Density based methods**
 - Introduce artificial compressibility to mimic compressible flows – Artificial compressibility methods.
 - Alternatively, solve continuity equation and use pre-conditioning to overcome the stiffness of the system.

PRESSURE BASED METHODS

› Pressure based methods

- Derive an equation for pressure based on discrete mass conservation or the continuity equation.
- Many variations – SIMPLE family of algorithms or pressure projection methods etc.
- SIMPLE algorithms – A predictor and corrector approach to resolve the pressure-velocity coupling in a segregated manner.

› Advantages

- More suitable for very low Mach number flows.
- Ensures better mass conservation.
- Faster solution possible.

PRESSURE BASED METHOD IN SU2

Momentum equation:

$$\mathbf{A}_{ij} \Delta U_j^* = R(U_i^n) - F_i^p$$

$$\mathbf{A}_{ij} = \left(\frac{|\Omega|}{\Delta t} \delta_{ij} + \frac{\partial R_i}{\partial U_j} \right), R(U) = F^v - F^c$$

Pressure correction equation:

$$-\sum_f \rho \frac{|\Omega|}{diag(\mathbf{A})} \cdot (\nabla P_f') \cdot \vec{n}_f = -\sum_f \dot{m}_f^*$$

Mass flux on the RHS found using:

$$\sum_f \dot{m}_f^* = \sum_f \rho \vec{U}_f^* \cdot \vec{n}_f$$

Face velocity found using momentum interpolation (Rhie-Chow) technique

$$U_f^* = \overline{U}_f^* - \frac{|\Omega|}{diag(\mathbf{A})} (\nabla P_f - \overline{\nabla P_f})$$

IMPLEMENTATION DETAILS

- › Upwind discretization (with MUSCL reconstruction)
- › Boundary conditions available – Velocity inlet, Pressure outlet, Wall, Inviscid wall, Freestream, Symmetry (from the recent pull request by @TobiKattmann)
- › Single core support no MPI yet.
- › Steady state solutions.
- › Local time stepping.

IMPLEMENTATION DETAILS

- › Available on the main repo in the 'feature_Pressure_based' branch (updated with develop regularly).
- › New config option –
`KIND_INCOMP_SYSTEM = (DENSITY_BASED, PRESSURE_BASED)`
- › Use existing driver structure routines.
- › Defined a new iteration class for the predictor corrector algorithm.
- › Adding new multigrid cycle to accommodate the predictor-corrector loop.
- › New set of files for solver, numerics and variable classes.
(`_direct_mean_PBinc.cpp`). Poisson solver classes still remain.

TEST CASES

1. Channel flow ($Re = 400$)
2. Laminar flow over a flat plate ($Re = 4 \times 10^5$)
3. Laminar flow over a cylinder ($Re = 40$ and $Re = 100$)
4. Laminar flow over a backward facing step ($Re = 800$)

CHANNEL FLOW

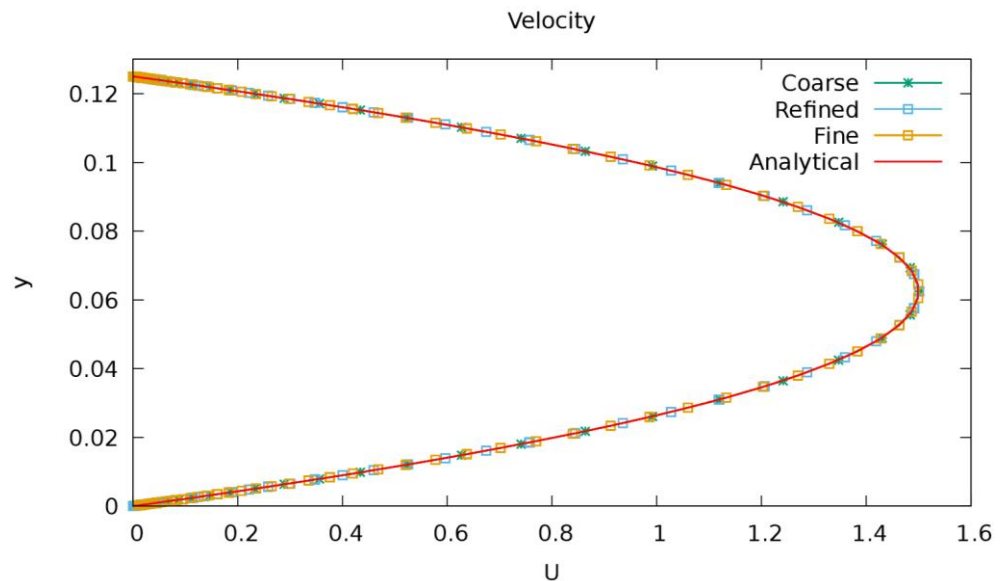
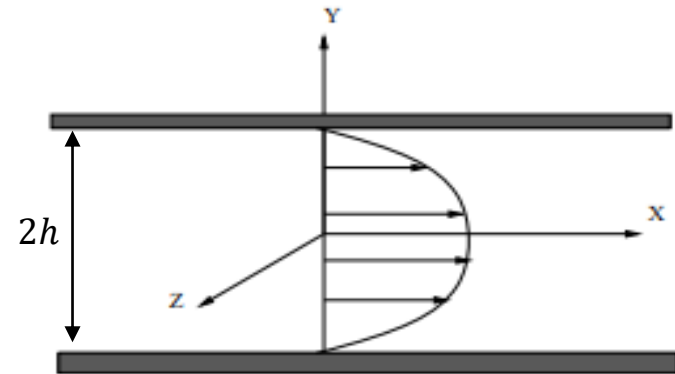
› Fully developed channel at $Re = 400$

› Velocity profile given by

$$u(y) = \frac{P}{2\mu}(h^2 - y^2)$$

$$v = 0$$

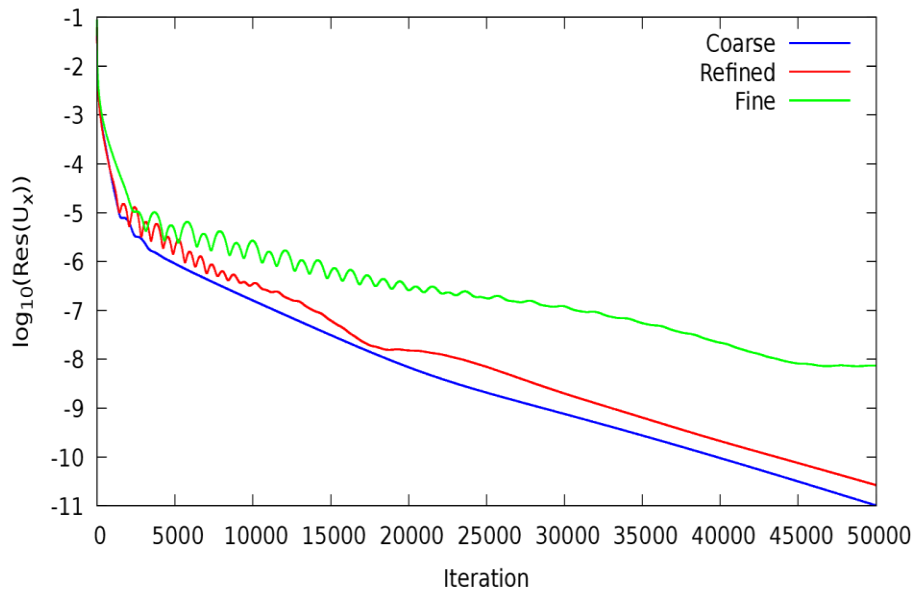
› $h = 0.0625$



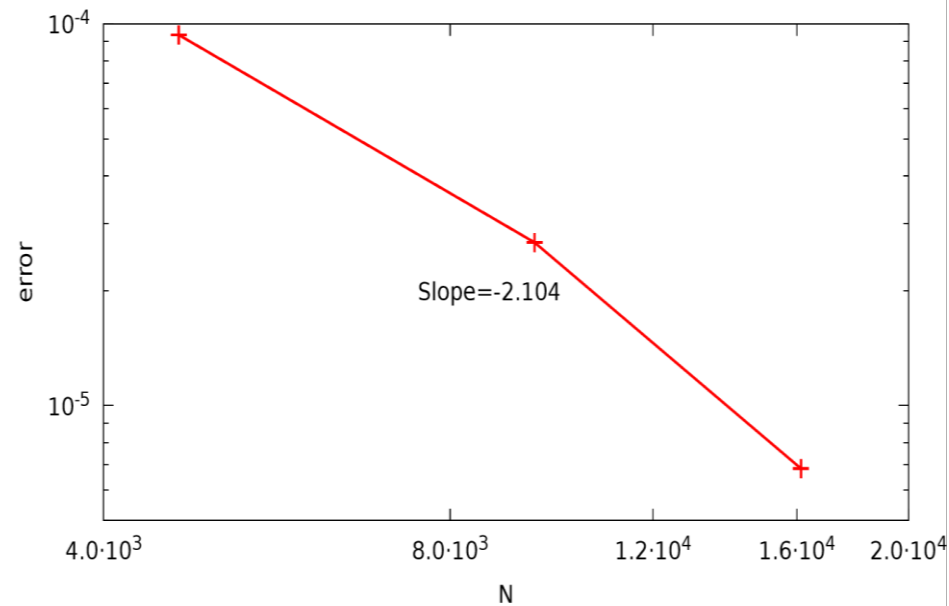
CHANNEL FLOW

- › 3 different grid resolutions
- › Order of accuracy based on the grid refinement study ~ 2

Convergence history, CFL=1

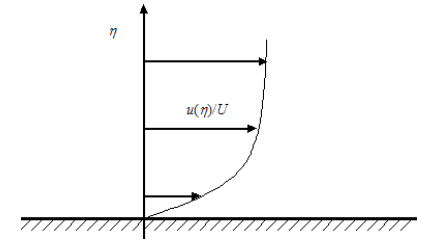


L2 error norm



LAMINAR FLAT PLATE

- › Steady laminar boundary layer at $Re = 4.0 \times 10^5$
- › Blasius equation – Assume zero pressure gradient and uniform outer flow. Define a scaled wall normal distance, η , and stream function ψ .
- › Based on the boundary layer equations, an ODE can be formed for the stream function which is solved numerically to obtain self similar solutions for the flow.

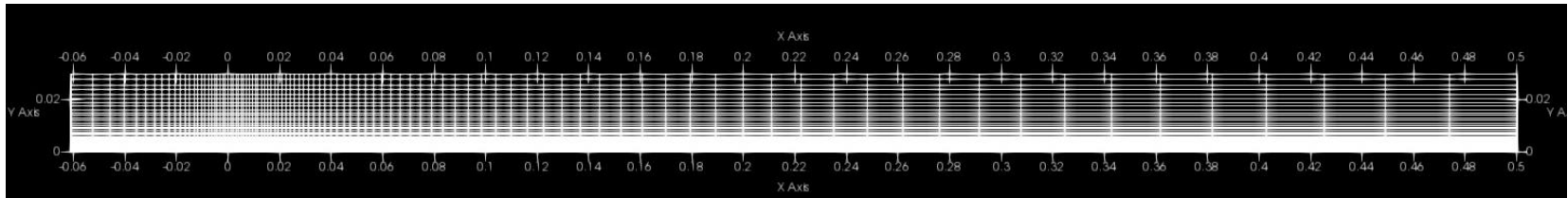


$$\eta = y \sqrt{\frac{U}{2\nu x}} \quad \psi = \sqrt{2\nu U x} f(\eta) \quad f''' + ff' = 0$$

LAMINAR FLAT PLATE

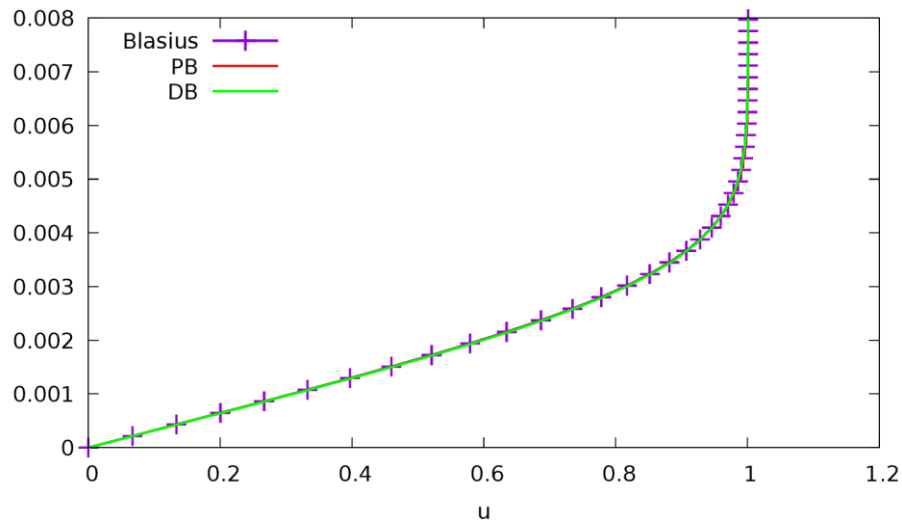
- › Solve the Blasius equations using the shooting method.
- › Compare numerical and Blasius solutions for velocity components at $x = 0.45$ and skin friction, c_f , along the length of the flat plate.

$$u(x, y) = Uf'(\eta) \quad v(x, y) = \sqrt{\frac{U\nu}{2x}} [\eta f'(\eta) - f(\eta)] \quad c_f = \frac{0.664}{\sqrt{Re_x}}$$

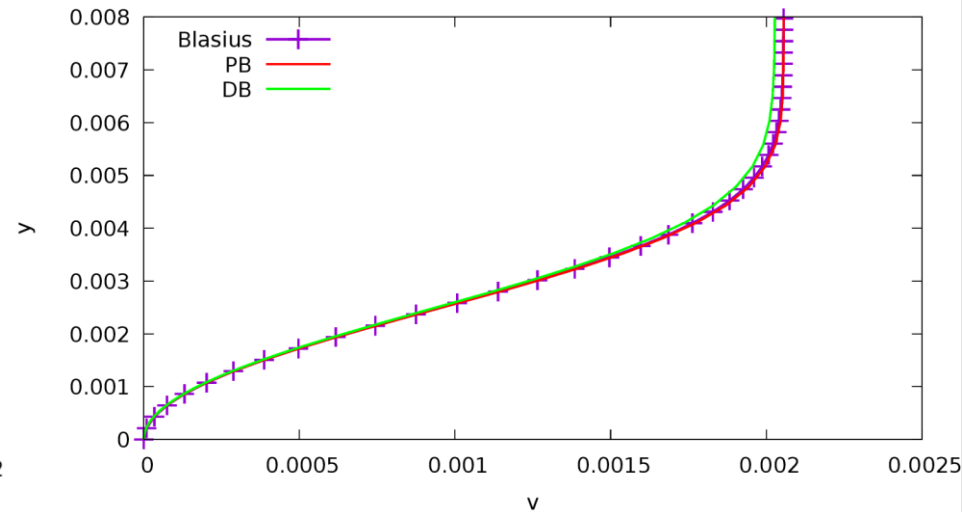


LAMINAR FLAT PLATE

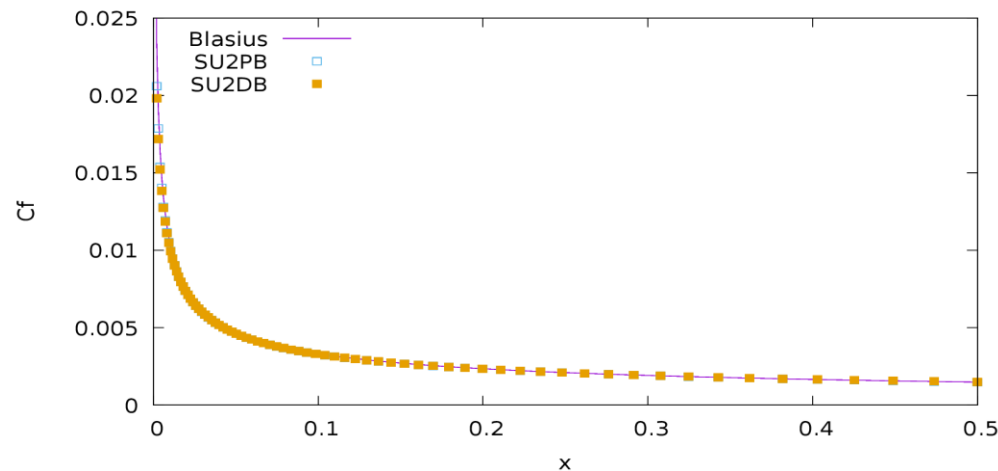
Numerical vs Blasius (u), $Re = 4e5$



Numerical vs Blasius (v), $Re = 4e5$

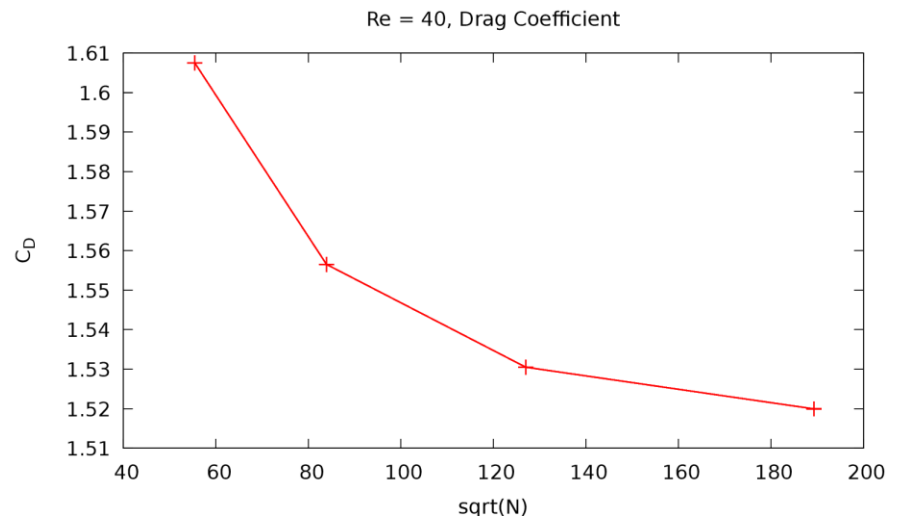
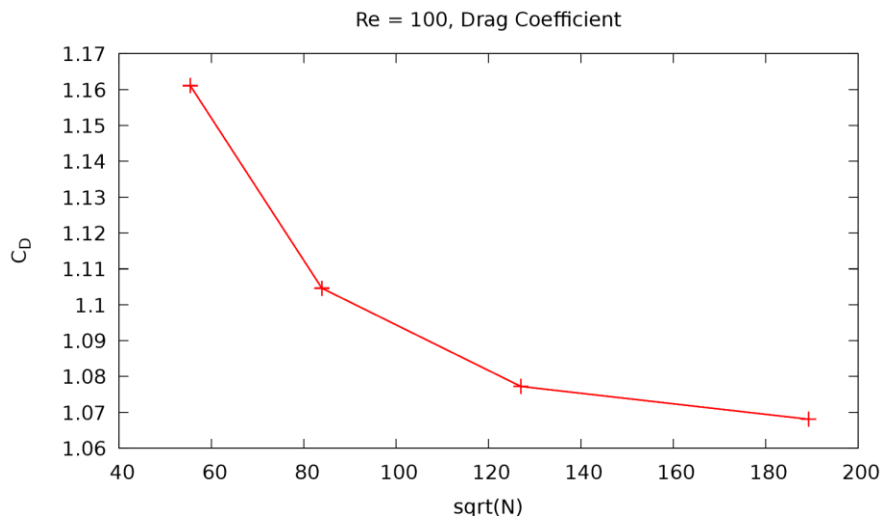
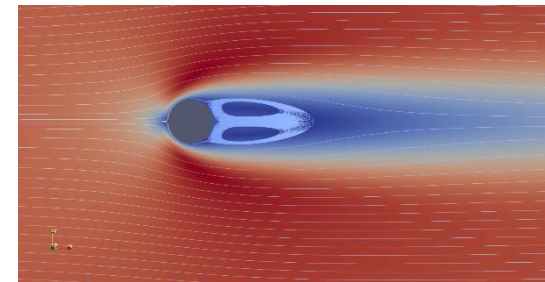


Skin friction, $Re = 4e5$

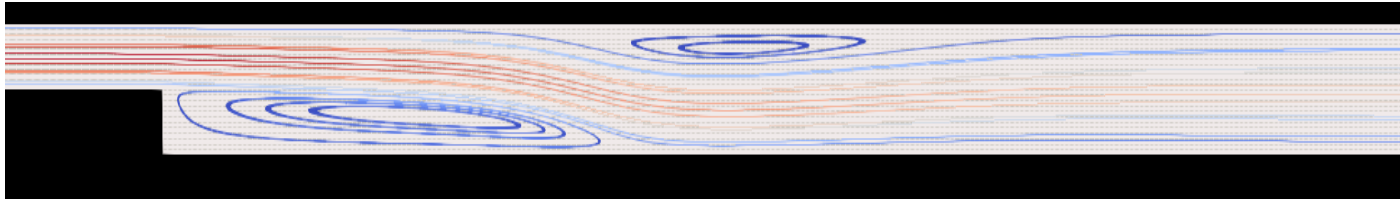


LAMINAR FLOW OVER A CYLINDER

- › Steady separated flow around a cylinder
- › $Re = 40$ and $Re = 100$
- › Compare drag for different grid resolutions.

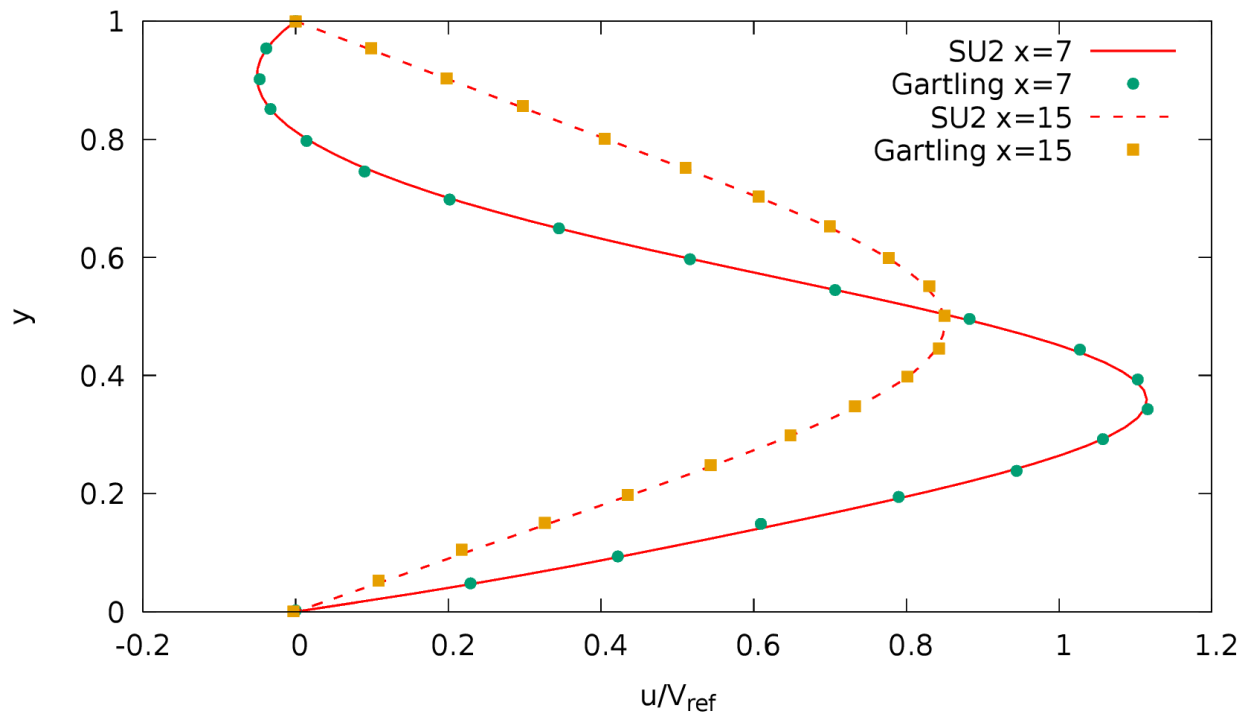


LAMINAR BACKWARD FACING STEP



- › Flow past a backward facing step at $Re = 800$.
- › Flow separates at the step and reattaches to the lower wall.
- › At $Re = 800$, a secondary eddy is formed along the upper wall.
- › Compare the numerical solution to Gartling, D. K. (1990), A test problem for outflow boundary conditions—flow over a backward-facing step. Int. J. Numer. Meth. Fluids, 11: 953-967.

LAMINAR BACKWARD FACING STEP



Reattachment length:

- Lower wall – $L_{lw} = 5.81$
- Upper wall – $L_{uw} = 5.69$

UPCOMING DEVELOPMENTS

- › Multigrid method.
- › RANS equations.
- › MPI support.
- › Unsteady problems.
- › Periodic BCs, ALE formulation.

› **THANK YOU FOR YOUR ATTENTION**

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