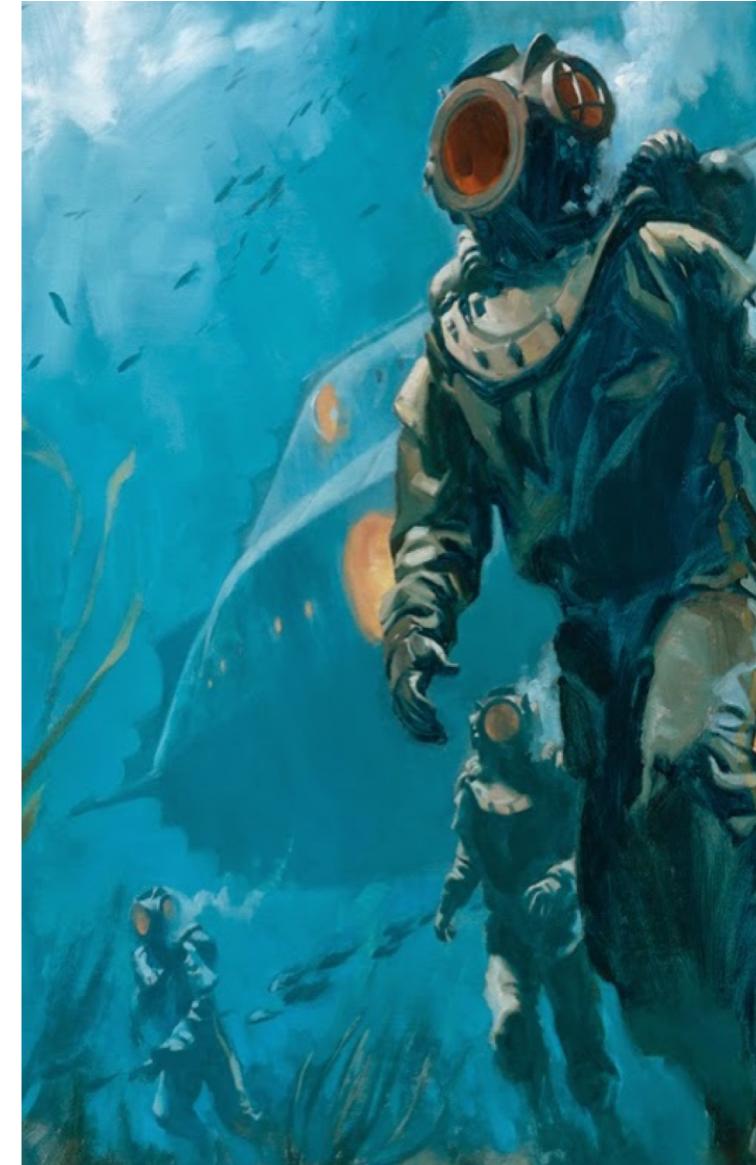


SU2-NEMO: NonEquilibrium MOdels for Hypersonic Flows

C. Garbacz, W. Maier, J. Needels, T. Economou, A. Loseille, B. Munguía, J.B. Scoggins, T. Magin, J.J. Alonso, G. Barrenechea, M. Fossati



Outline

SU2

1. Multi-species multi-temperature solver
2. Update to “develop” and regression tests (C. Garbacz)
3. Turbulence modeling (W. Maier)
4. Ionization modeling (J. Needels)
5. Adaptive solutions (A. Loseille, B. Munguía)

Ambition and objectives

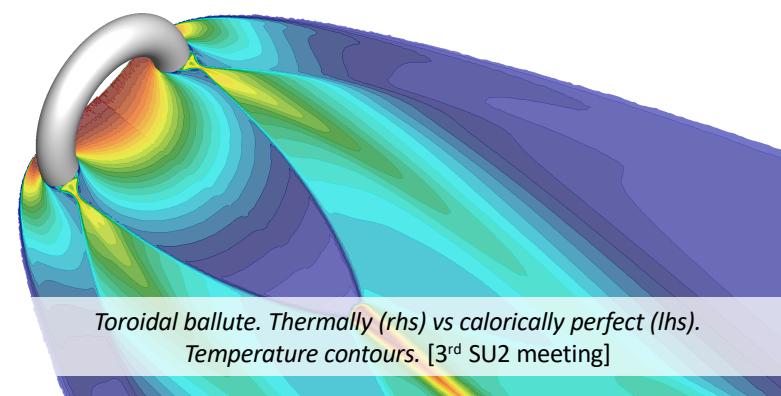
SU2

"Enhance the multi-physics capabilities of SU2 and extend the spectrum of applications, with a focus on design"

- Reboot modeling of high-temperature effects using latest versions of SU2
- Define roadmap for coordinated development of thermochemistry and nonequilibrium models
- Incorporate advanced models for finite-rate chemistry and thermal nonequilibrium
- Consolidate implementation and use of advanced thermodynamic models



X43 vehicle. Thermally (rhs) vs calorically perfect (lhs).
Temperature contours. [2nd SU2 meeting]



Toroidal ballute. Thermally (rhs) vs calorically perfect (lhs).
Temperature contours. [3rd SU2 meeting]

Some background equations and models

SU2

$$\frac{\partial \rho_s}{\partial t} + \nabla \cdot (\rho_s \vec{u} - \rho_s \vec{u}_{d,1}) = \dot{w}_s$$

$$\frac{\partial \rho \vec{u}}{\partial t} + \nabla \cdot (\rho \vec{u} \otimes \vec{u} + P \bar{I} - \bar{\tau}) = 0$$

$$\frac{\partial \rho e}{\partial t} + \nabla \cdot (\rho e \vec{u} + P \bar{I} \cdot \vec{u} - \bar{\tau} \cdot \vec{u} + \vec{q}) = \nabla \cdot (- \sum_s h_s \rho_s \vec{u}_{d,s}) - \nabla \cdot \vec{q}_v$$

$$\frac{\partial \rho e_v}{\partial t} + \nabla \cdot (\rho e_v \vec{u} + \vec{q}_v + \sum_s e_{v,s} \rho_s \vec{u}_{d,s}) = \sum_s Q_s^v + \sum_s Q_S^{t-v}$$

$$P = P(\rho_s, T)$$

$$e = e(X_s, T)$$

$$\rho e_v = \sum_s \rho_s e_{v,s}$$

$$\vec{q}_v = -k_v \nabla T_v$$

$$e_{v,s} = \frac{R}{W_s} \frac{\theta_{v,s}}{\exp(\theta_{v,s}/T_v) - 1}$$

$$\tau_{ij} = \mu \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) - \frac{2}{3} \mu \delta_{ij} \nabla \cdot \vec{u}$$

$$\vec{q} = -k \nabla T$$

$$\mu = \sum_s \frac{\mu_s X_s}{\phi_s}, \quad k = \sum_s \frac{k_s X_s}{\phi_s}$$

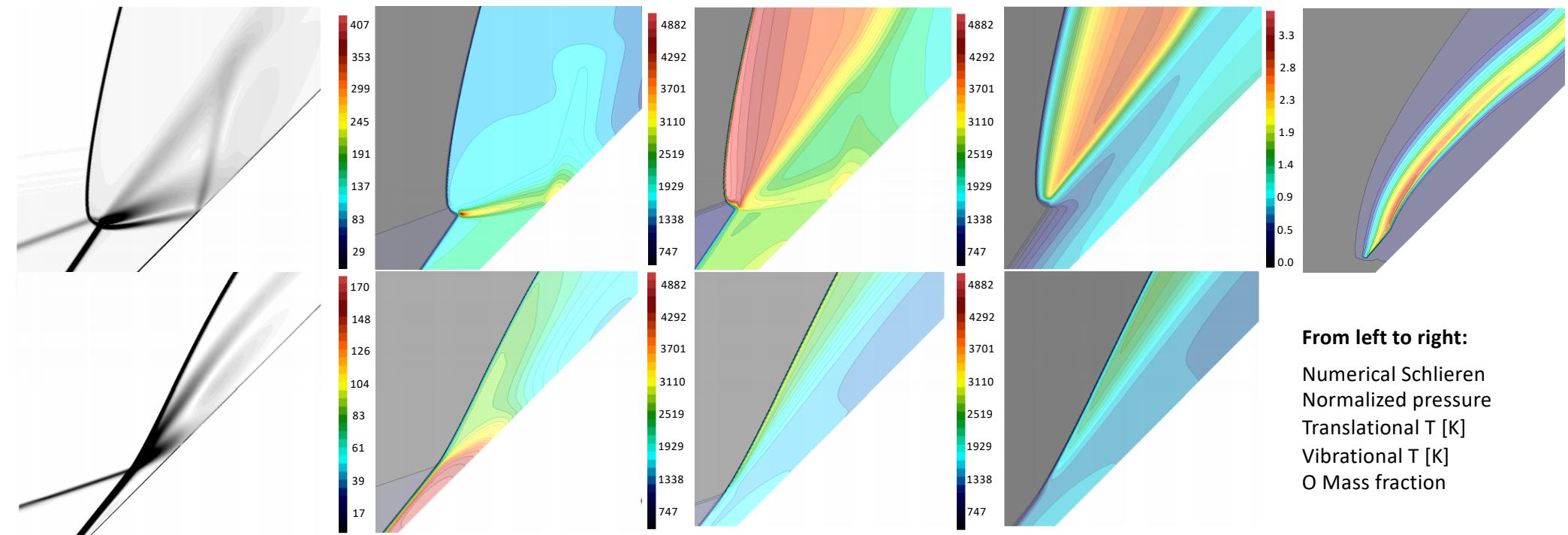
Initial efforts by Sean Copeland (PhD, 2015, Stanford University): “A Continuous Adjoint Formulation for Hypersonic Flows in Thermochemical Nonequilibrium”

... but **SU2** has continued to evolve ... new and more general implementation needed!

Shock interference patterns on double wedges (c. Garbacz)

SU2-NEMO with Mutation++

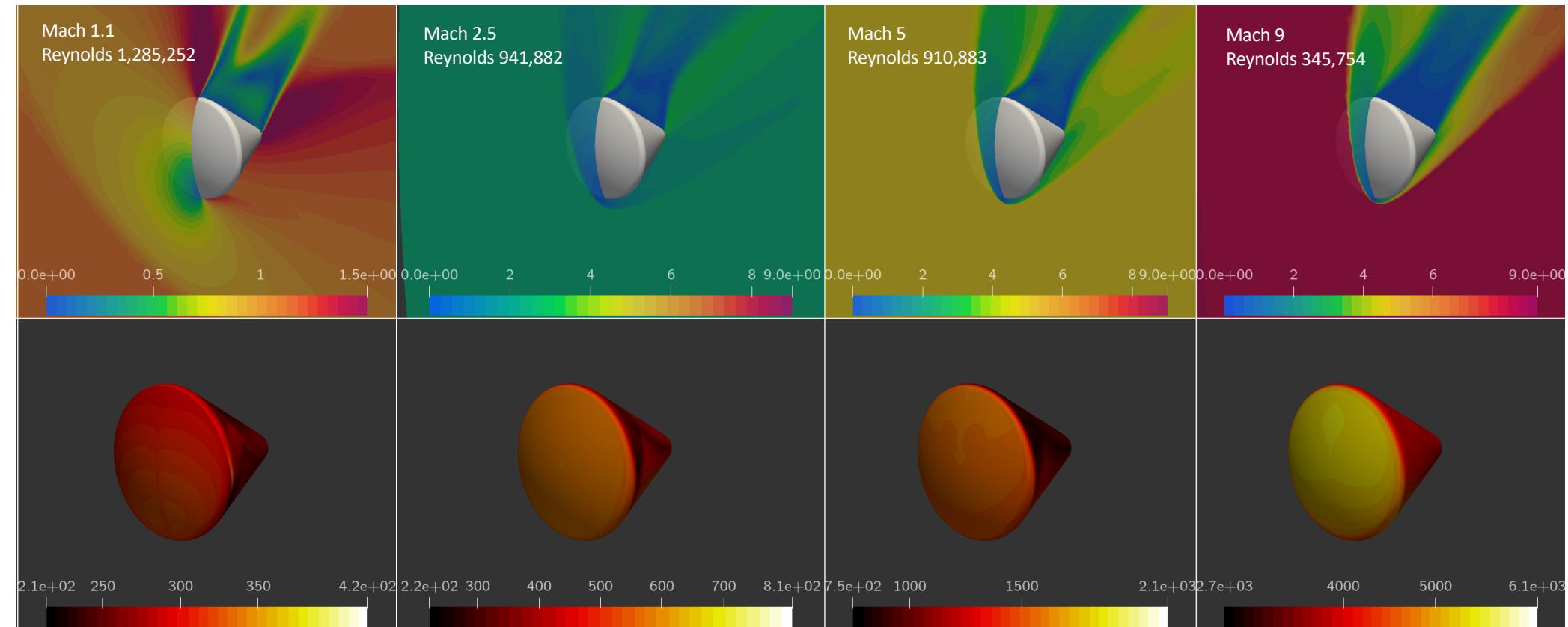
SU2



Simulation of a hypersonic Mach 9 flow over a double wedge. Shock interaction patterns with thermal nonequilibrium and finite-rate chemistry. Air-5 top, CO₂-N₂ bottom

Apollo command module at 45deg (C. Garbacz, W. Maier)

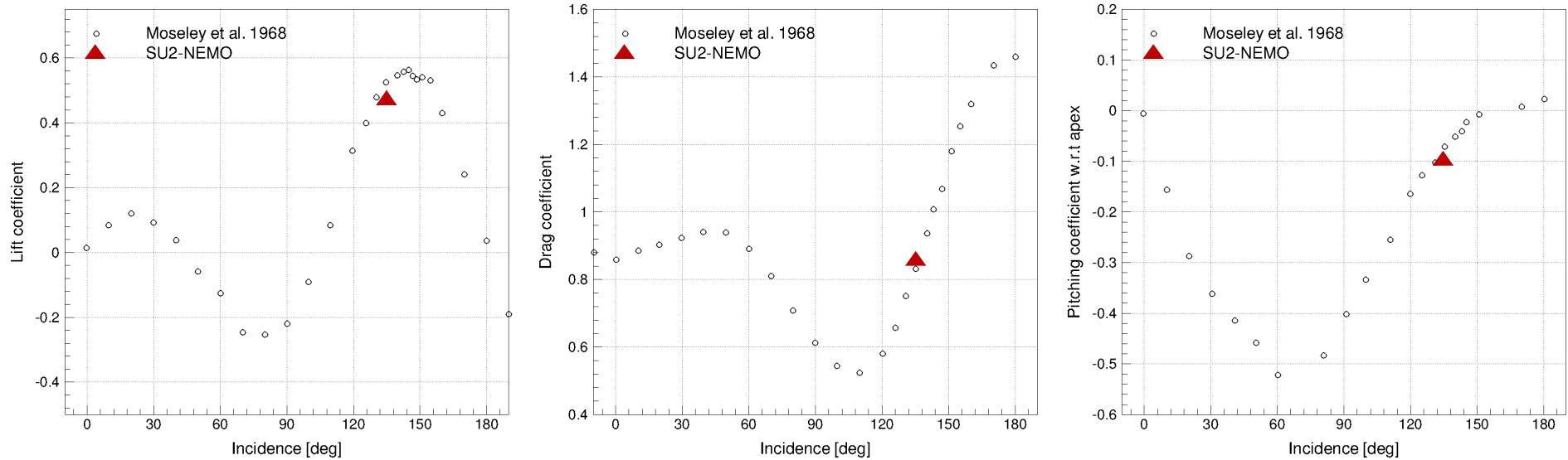
SU2



Mach number contours (top row), Temperature [K] (bottom row)

Apollo command module at 45deg (C. Garbacz, W. Maier)

SU2

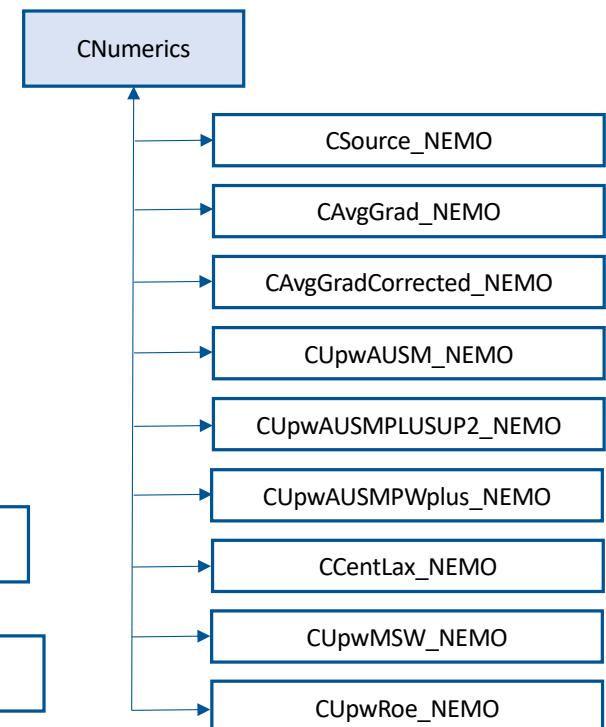
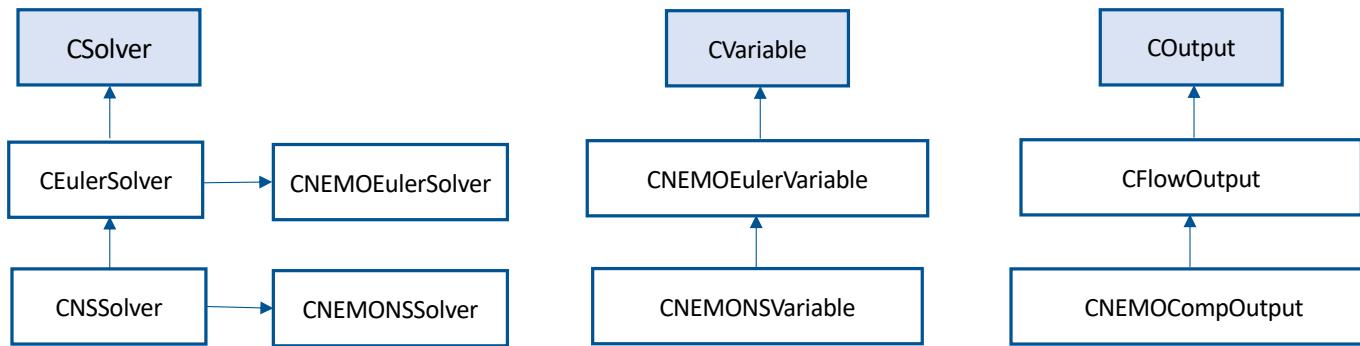


Aerodynamic coefficients for Mach 2.5 case

Update to “develop” (C. Garbacz) SU2-NEMO

SU2

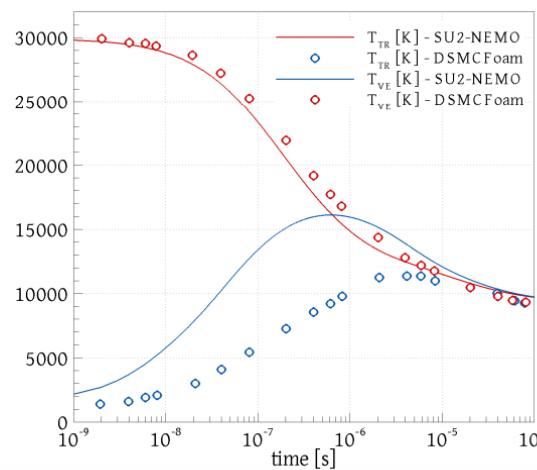
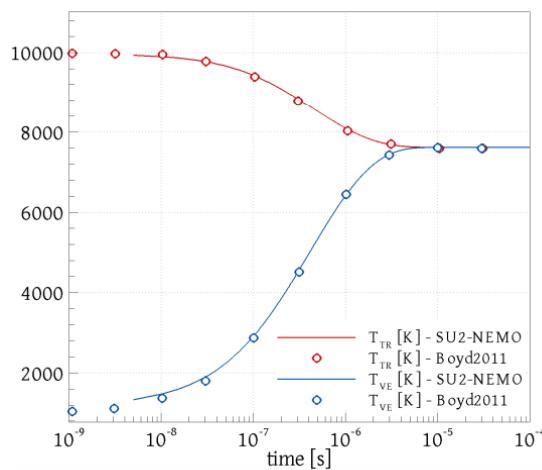
- File/Class restructuring
- Generic v7 routines – gradient computation, limiters, ...
- Improvements for performance



Update to “develop” (C. Garbacz)

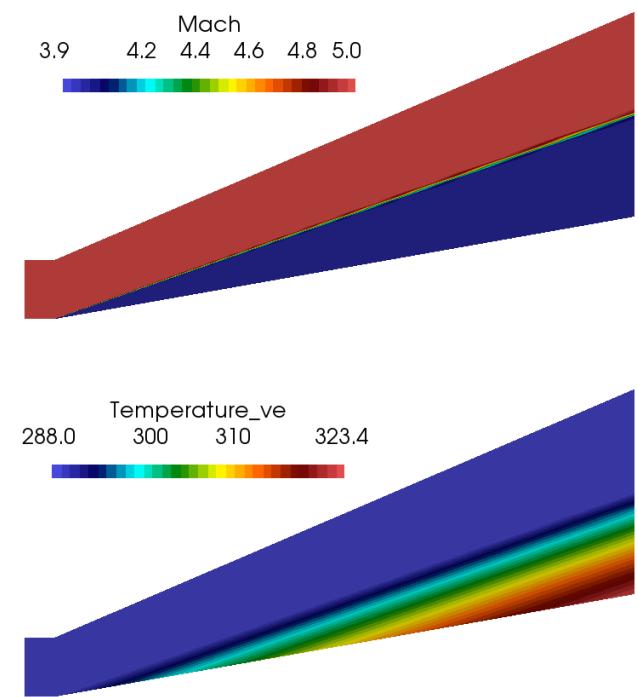
Regression test cases

SU2



0D adiabatic heat bath with relaxation and finite-rate chemistry (N_2-N)

Reaction Mechanism	Frozen	$N_2 + N_2 \rightarrow 2 N + N_2$
T_{tr} [K]	10,000	30,000
T_{ve} [K]	1,000	1,000



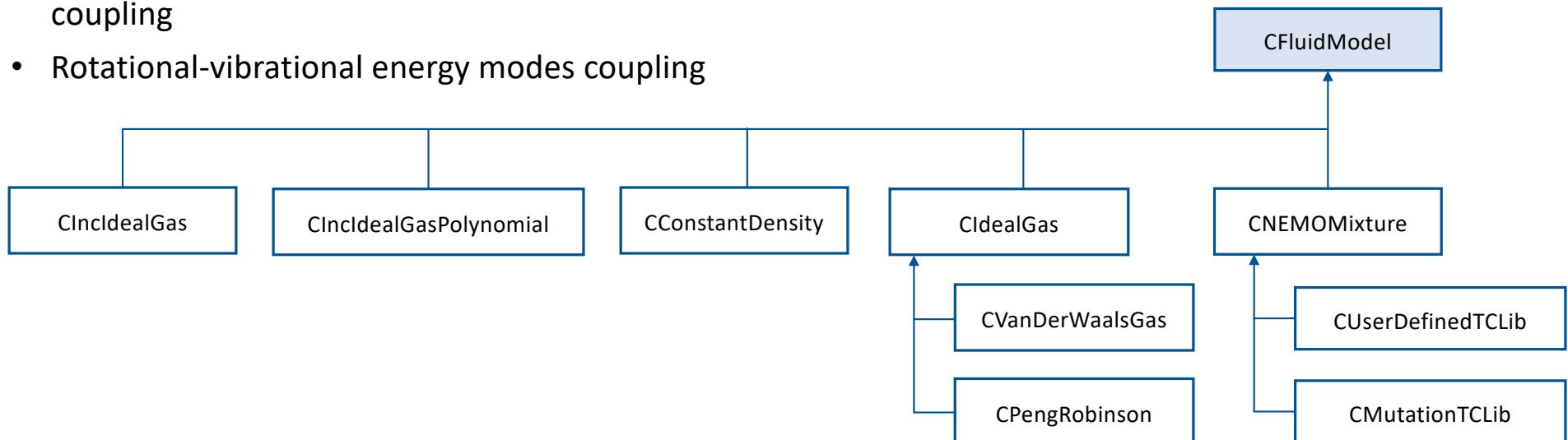
2D Mach 5 inviscid flow over a 10° wedge

Update to “develop” (C. Garbacz)

Roadmap

SU2

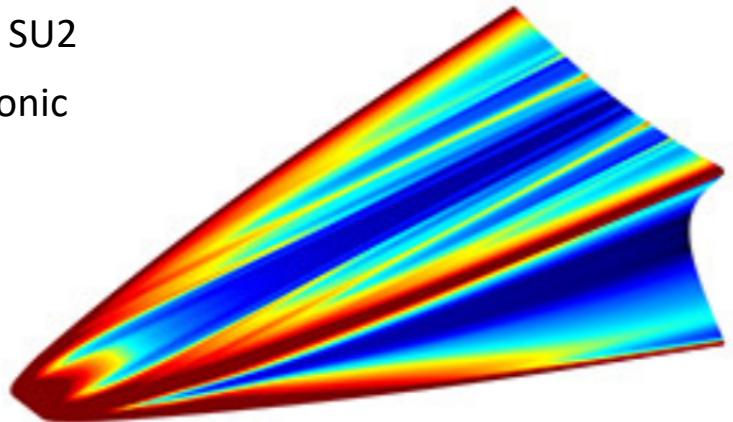
- Incorporate **CFluidModel** class to handle all mixture-related computations (thermodynamics, chemistry, transport)
- Merge link **SU2-NEMO — Mutation++**
- Preferential vs. non-preferential modeling of vibration-chemistry coupling
- Rotational-vibrational energy modes coupling



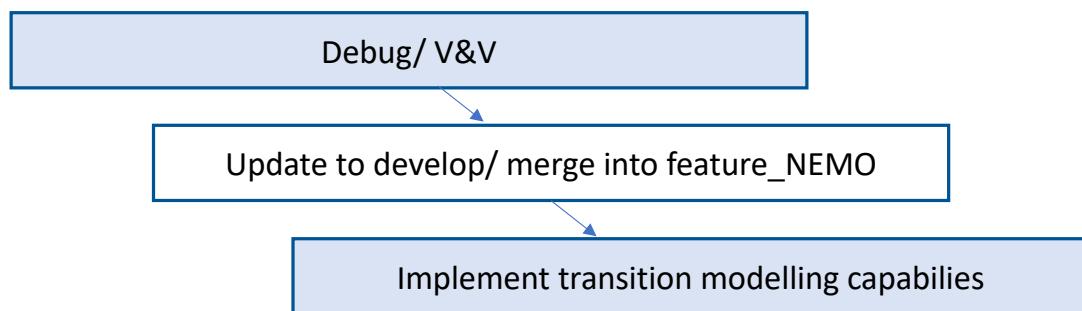
Turbulence modeling (w. Maier)

SU2

- Make use of the existing turbulence model structure within SU2
- SA-Catris, SA-Neg, and SST-V models are standard in hypersonic flows (e.g., US3D)
- Currently in debugging phase.



Steps forward:

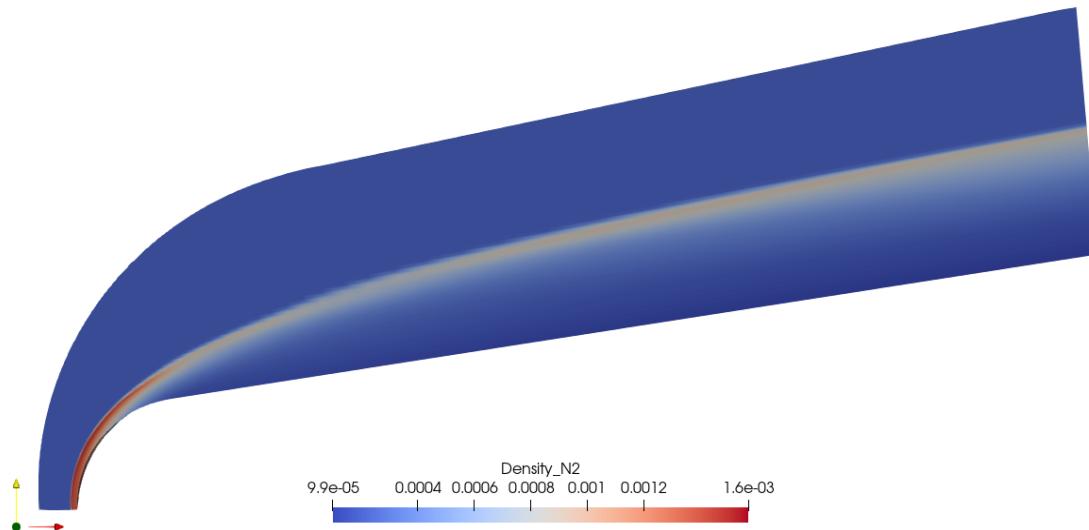


Bolt Surface Heat Transfer Rate
<https://cse.umn.edu/aem/computational-hypersonics-research-lab>

Ionization modeling (J. Needels)

SU2

- Implementation of 7-species air chemistry model to capture ionization effects during hypersonic re-entry
- Validation against experimental data (RAM-C II flight experiment)
- Air-11 model implemented, validation in progress



Test Case: RAM-C II 7,936 Element 3D Hexahedral Mesh

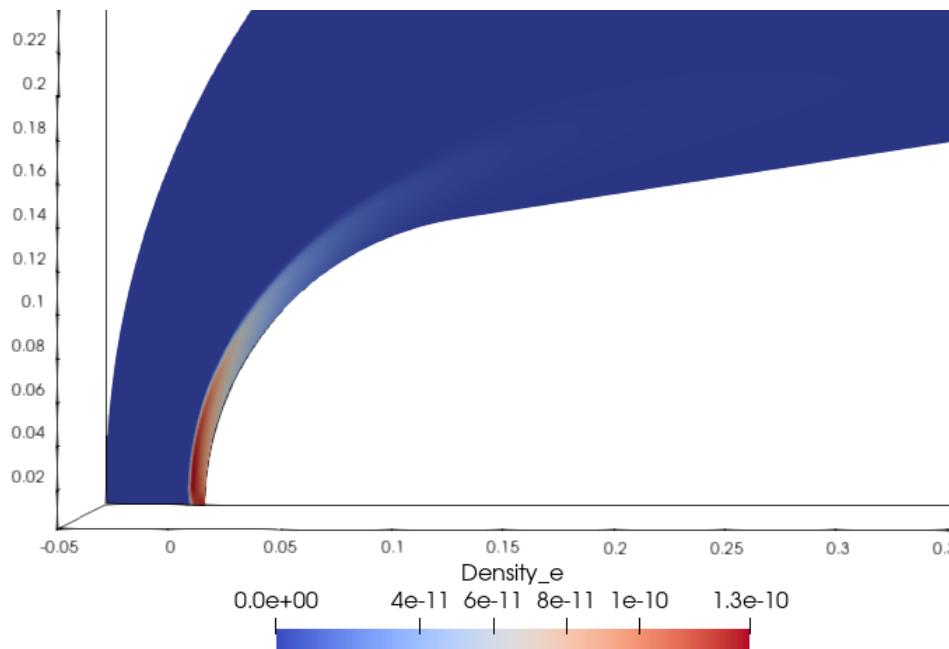
SU2 - NonEquilibrium MOdels

Free-stream Parameter	Value
Altitude [km]	61
M	23.9
T [K]	254
P [Pa]	19.8
Kn	0.0012

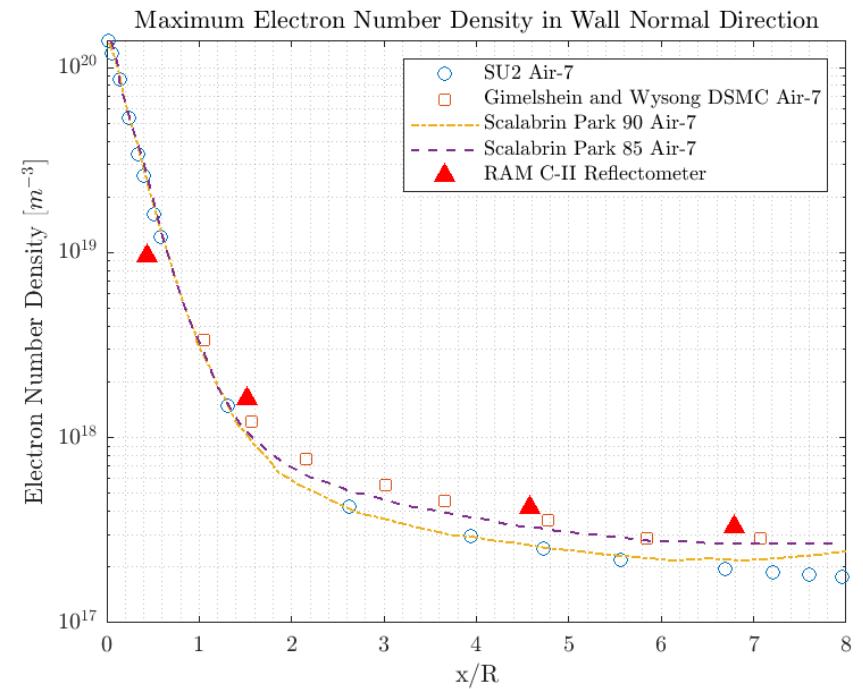
7-Species Air Chemistry Model:
 $S : \{N_2, O_2, N, O, NO, NO+, e-\}$

Ionization modeling (J. Needels)

SU2



Electron Density over 3D RAM-C II Forebody $M = 23.9$

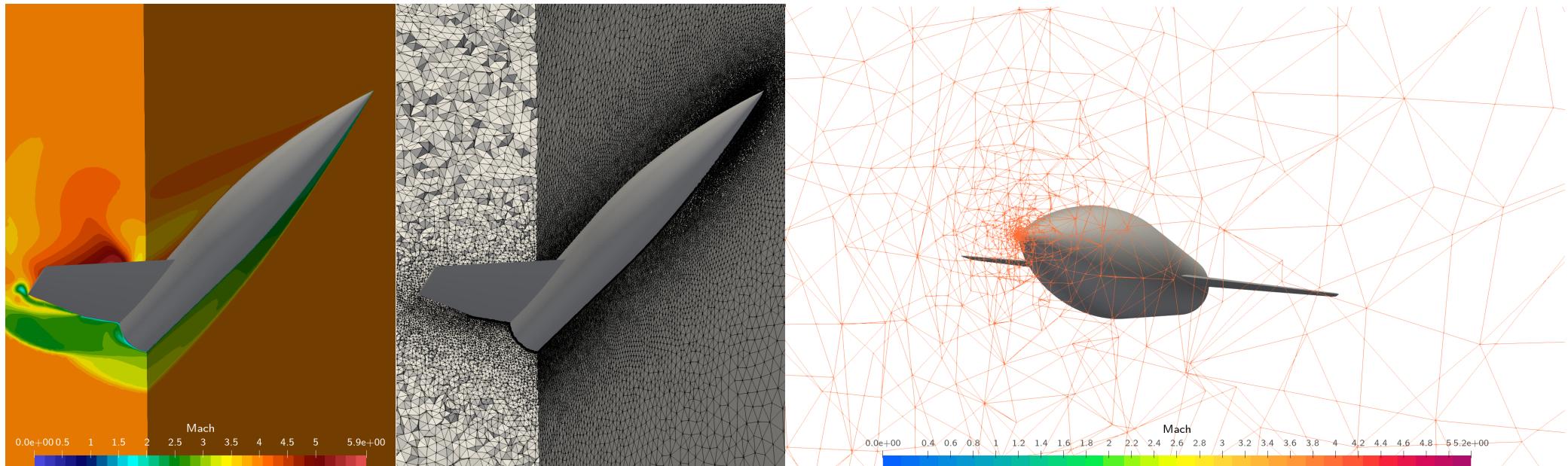


Comparison with Numerical Results and Flight Data

SU2-NEMO + AMG library for viscous flows (A. Loseille, B. Munguía)

SU2

Mach 4 flow over a wing-body configuration (Bedford vehicle) at 20deg incidence



Original mesh/solution

Nodes: 3,109,217

Elements: 11,473,410 (prisms, pyramids, tets)

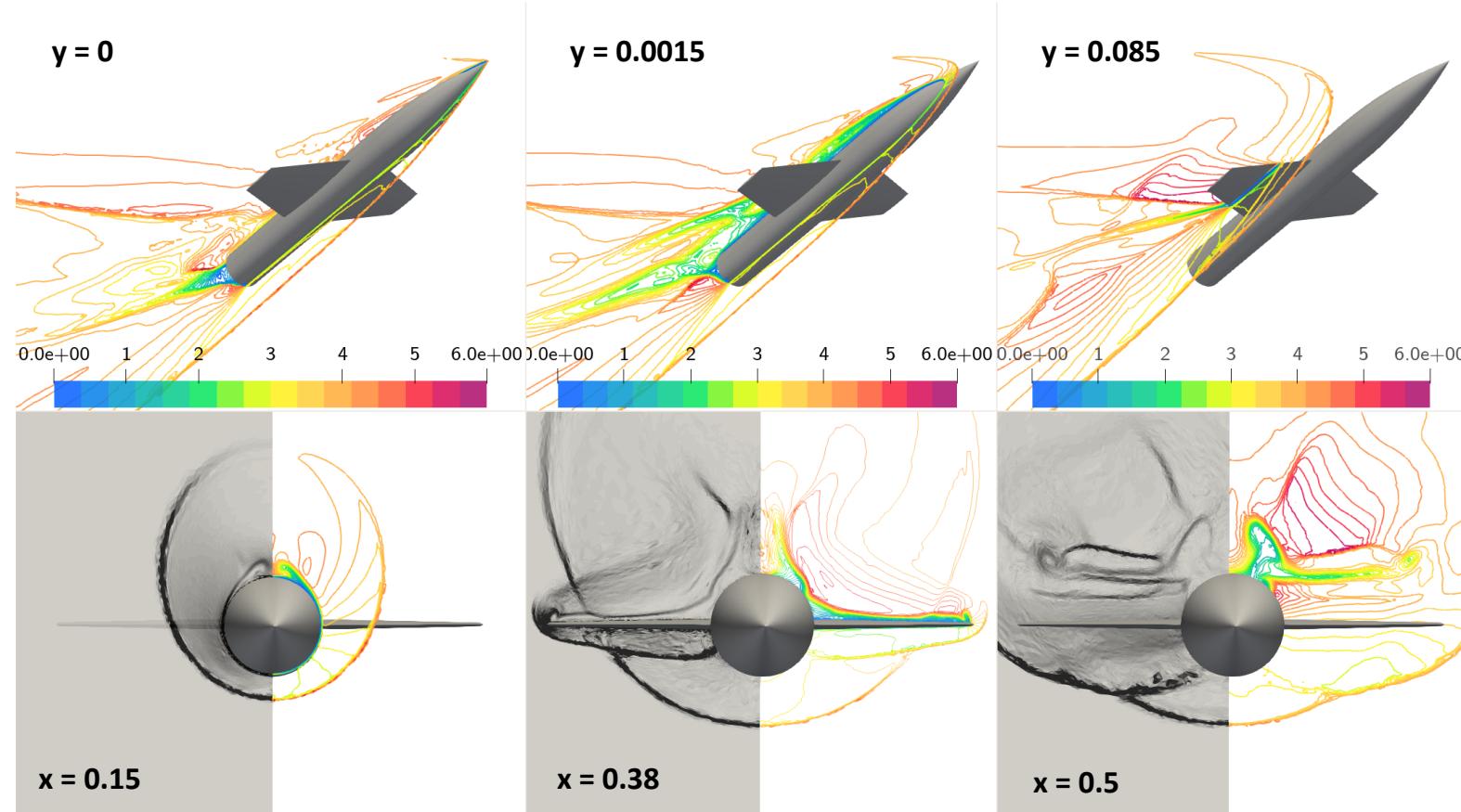
Adapted mesh/solution

Nodes: 2,111,391

Elements: 10,699,929 (prisms, pyramids, tets)

SU2-NEMO + AMG library for viscous flows (A. Loseille, B. Munguía)

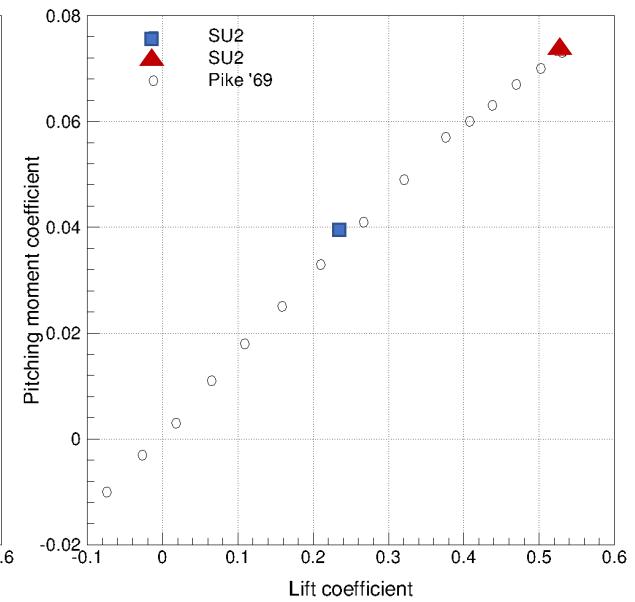
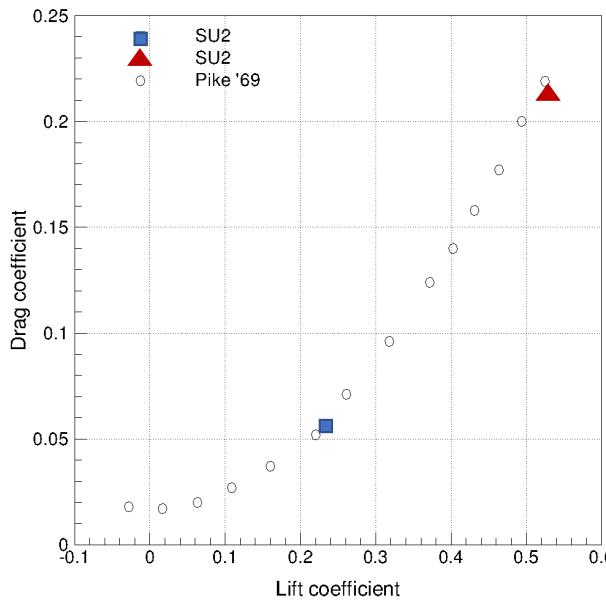
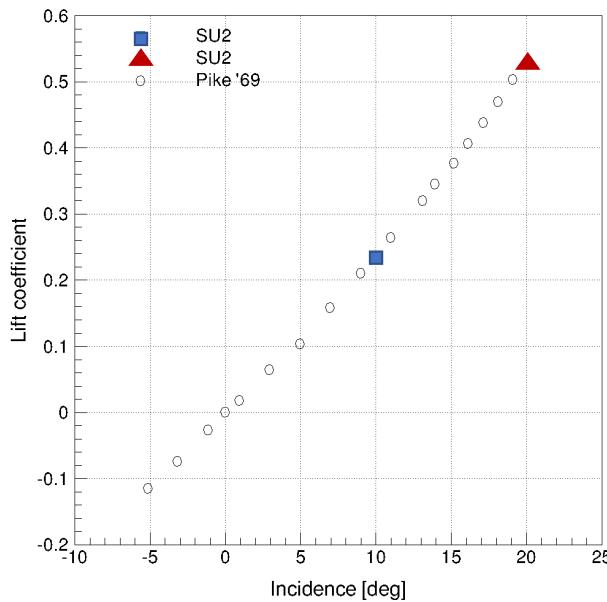
SU2



Mach number contours and Numerical Schlieren

SU2-NEMO + AMG library for viscous flows (A. Loseille, B. Munguía)

SU2



Reference area	0.04021 m ² (/2)
Reference length	0.15207 m (MAC)
Point for C _{M_y}	0.318 m

	C _L	C _D	C _{M_y}
10°	0.23438	0.06242	0.04013
20°	0.52490	0.21944	0.074768

Pike, J., Wind Tunnel Tests on Six Wing-Body Models at $M = 4$, Ministry of Technology, Aeronautical Research Council, 1969

A little ways down the road ...

SU2

- Vibration-dissociation modeling
- Advanced turbulence modeling
- Ionization and magneto-gasdynamics effects
- Advanced thermal boundary conditions (e.g. equilibrium radiation)
- Coupling with 6-DOF model and fragmentation for re-entry problems

1. Gomes, A.C., Fossati, M., Maier, T., Alonso, J.J., Scoggins, J.B., Magin, T., Economou, T. (2020). **Numerical Study of Shock Interference Patterns for Nonequilibrium Gas Flows**. AIAA 2020 Scitech Forum and Exposition. Orlando (FL), US. January. <https://doi.org/10.2514/6.2020-1805>
2. Gomes A.C., Maier, T., Alonso, J.J., Scoggins, J.B., Magin, T., Economou, T., G. Barrenechea and Fossati, M. **Shock Interactions in Inviscid Air and CO₂-N₂ Flows in Thermochemical Nonequilibrium**. Shock waves. *Under review*
3. Gomes A.C., Maier, T., Alonso, J.J., Scoggins, J.B., Magin, T., Economou, T., B. Munguia, A. Loseille, G. Barrenechea and Fossati, M. **Nonequilibrium Shock Interference Patterns over Hypersonic Vehicles**. *In preparation*
4. Gomes A.C., Maier, T., Alonso, J.J., Scoggins, J.B., Magin, T., Economou, T., G. Barrenechea and Fossati, M. **Characterization of shock wave interaction for Viscous Air and CO₂ Flows in Thermochemical Nonequilibrium**. *In preparation*

