

ADJOINT-BASED DESIGN OPTIMIZATION OF POLLUTANT EMISSIONS IN HEAT EXCHANGERS



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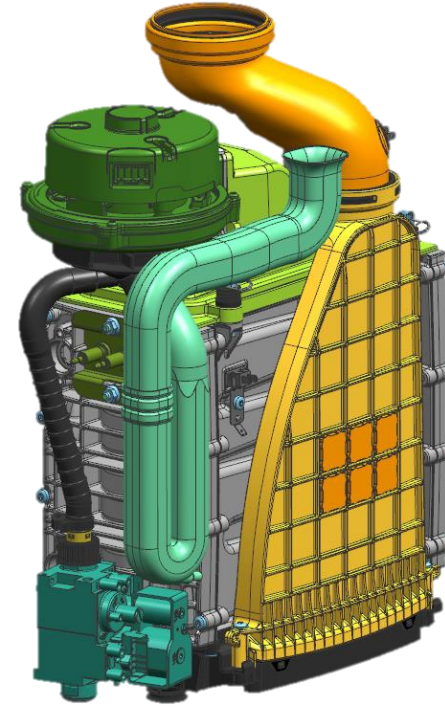
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Motivation

Natural gas boilers for domestic heating



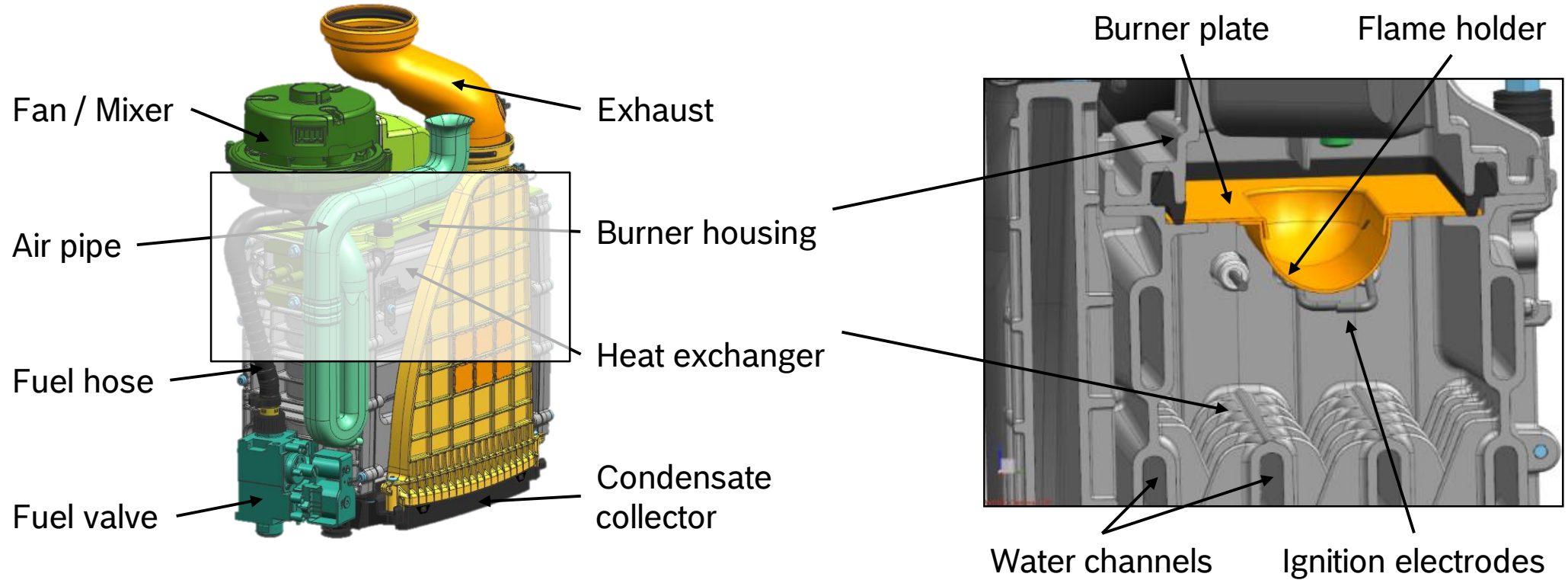
Wall hanging appliance



CAD model of the heat cell

Motivation

Working principle

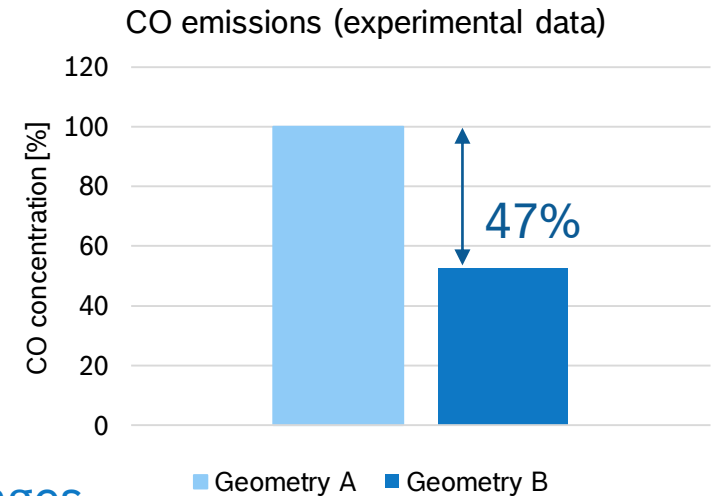
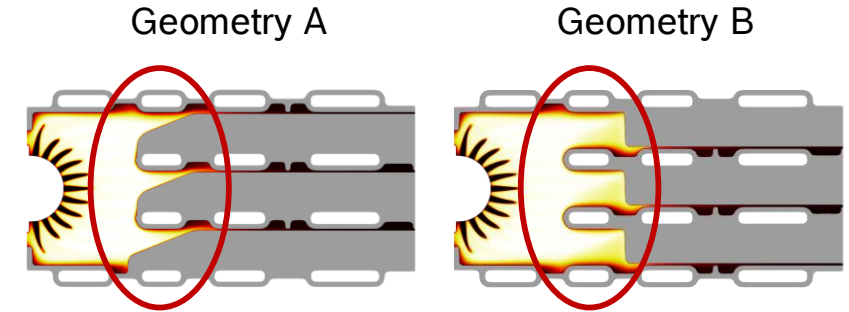


Combustion regime: Laminar, premixed methane gas combustion

Motivation

Reduction of pollutant emissions

- ▶ During combustion harmful pollutants CO and NO_x are formed
- ▶ CO and NO_x emissions have to be reduced
- ▶ CO and NO_x emissions are strongly dependent on heat exchanger geometry
 - ▶ Emissions reduction is major driver for heat exchanger design
- ▶ CO and NO_x formation are counteracting processes
 - ▶ Difficult to reduce both CO and NO_x at the same time
- ▶ Additional constraints:
 - ▶ Thermal efficiency
 - ▶ Pressure drop
 - ▶ Manufacturing constraints like material thickness, casting process, ...



Adjoint optimization is a powerful tool in overcoming these challenges

COMBUSTION MODELLING

DETAILED CHEMISTRY MODELLING
THE FLAMELET PROGRESS VARIABLE (FPV) APPROACH
WORKFLOW / TOOL CHAIN

MODEL IMPLEMENTATION IN SU2

ARCHITECTURE
CONFIGURATION
MODEL VALIDATION

APPLICATION TO ADJOINT OPTIMIZATION

CASE SETUP
GEOMETRICAL DEFORMATION CONSTRAINTS
AUTOMATED REMESHING
RESULTS

OUTLOOK

Combustion modeling

Detailed chemistry simulations

Conservation equations:

$$\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{u}) = 0,$$

$$\frac{\partial(\rho \mathbf{u})}{\partial t} + \nabla \cdot (\rho \mathbf{u} \otimes \mathbf{u}) + \nabla p - \nabla \cdot \boldsymbol{\tau} = 0,$$

Species transport

$$\frac{\partial(\rho Y_i)}{\partial t} + \nabla \cdot (\rho \mathbf{u} Y_i) + \nabla \cdot (\rho \mathbf{V}_i Y_i) = \dot{\omega}_i,$$

$$\frac{\partial(\rho c_p T)}{\partial t} + \nabla \cdot (\rho \mathbf{u} c_p T) - \nabla \cdot (\lambda \nabla T) + \rho \nabla T \cdot \sum_{i=1}^n c_{p,i} Y_i \mathbf{V}_i = \dot{\omega}_T$$

Coupled system:

$$\dot{\omega}_i = W_i \sum_{r=1}^{n_r} \nu_{i,r} K_r \prod_{j=1}^{n_{sp}} \left(\frac{\rho Y_j}{W_j} \right)^{\nu'_{j,r}}$$

Expensive transport quantities:

$$\eta_{mix} = \sum_{i=1}^{n_{sp}} \frac{X_i \eta_i}{\sum_{j=1}^{n_{sp}} X_j \phi_{ij}}$$

- ▶ Mechanism used here: GRI-Mech 2.11 from UC Berkeley^[1]
- ▶ It contains 49 species and 277 elementary reactions
- ➔ Computational costs become challenging if applied in a design cycle

Combustion modeling

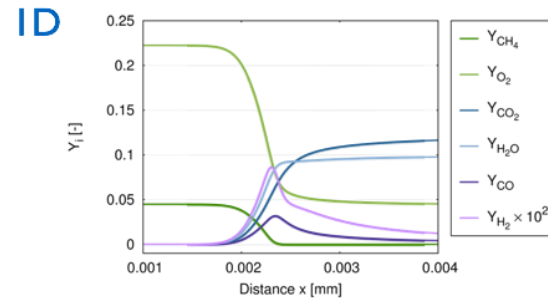
The flamelet progress variable (FPV) approach

Idea: Precompute 1D flames using detailed chemistry data, parameterize chemistry, and apply lookup method instead of solving chemistry.

Lookup parameters here:

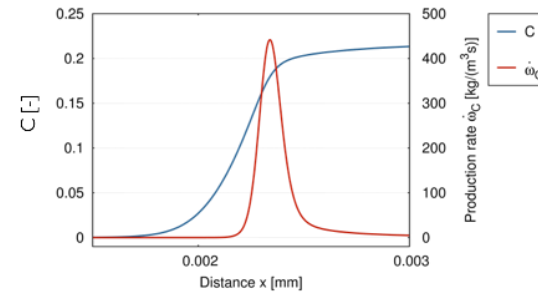
Progress variable C and enthalpy h

- Compute 1D simulations
- Tabulate 1D solutions as functions of progress variable C and enthalpy h
- Solve 3D transport equations for C and h using table lookups to obtain values for source terms and physical quantities



$$C = Y_{\text{CO}_2} + Y_{\text{H}_2\text{O}}$$

$$\dot{\omega}_C = \dot{\omega}_{\text{CO}_2} + \dot{\omega}_{\text{H}_2\text{O}}$$

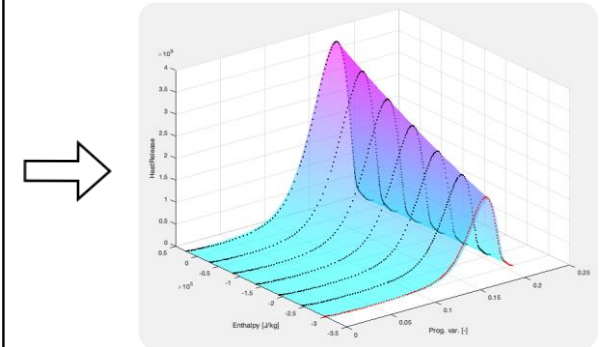


3D

$$\frac{\partial(\rho C)}{\partial t} + \vec{\nabla} \cdot (\rho \vec{v} C) - \vec{\nabla} \cdot (\rho \mathcal{D}_C \vec{\nabla} C) = \rho \dot{\omega}_C$$

$$\frac{\partial(\rho h)}{\partial t} + \vec{\nabla} \cdot (\rho \vec{v} h) - \vec{\nabla} \cdot (\rho \mathcal{D}_h \vec{\nabla} h) = \rho \dot{\omega}_h$$

$C, \text{Enthalpy } (h)$
 \downarrow
 \uparrow
 $\dot{\omega}(C, h)$
 $\nu(C, h)$
 $\rho(C, h)$
 $\mathcal{D}(C, h)$
 \dots



Combustion modeling

Emission models

Accuracy of Y_{CO} and Y_{NO} in the lookup table can be low for strong cooling.

➔ Transport equations for Y_{CO} and Y_{NO} with source term correction^[2]

Consider generic reaction equation for emission consumption:

Reaction # c : $EM + B \rightarrow C + D$, with $EM = \{\text{CO}, \text{NO}\}$

$$\dot{\omega}_{EM} = W_{EM} \sum_{r=1}^{n_r} v_{EM,r} K_r \prod_{j=1}^{n_{sp}} \left(\frac{\rho Y_j}{W_j} \right)^{v'_{j,r}} = \underbrace{W_{EM} \sum_{r=1, r \neq c}^{n_r} v_{EM,r} K_r \prod_{j=1}^{n_{sp}} \left(\frac{\rho Y_j}{W_j} \right)^{v'_{j,r}}}_{\dot{\omega}_{EM}^+} + \underbrace{W_{EM} K_c \rho^2 \frac{Y_{EM}}{W_{EM}} \frac{Y_B}{W_B}}_{\dot{\omega}_{EM}^-}$$

$$\dot{\omega}_{EM}^{3D} = \boxed{\dot{\omega}_{EM}^{+,1D}} + \boxed{\frac{\dot{\omega}_{EM}^{-,1D}}{Y_{EM}^{1D}}} \boxed{Y_{EM}^{3D}}$$

Stored in chemistry table

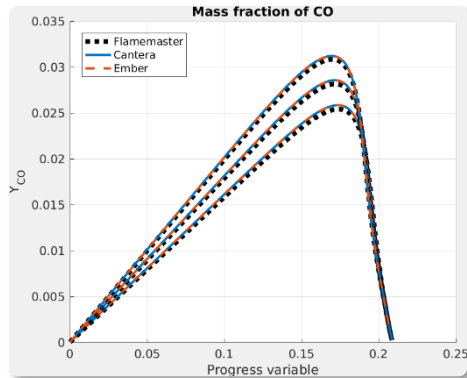
Solved using transport equation

Combustion modeling

Workflow / Tool chain

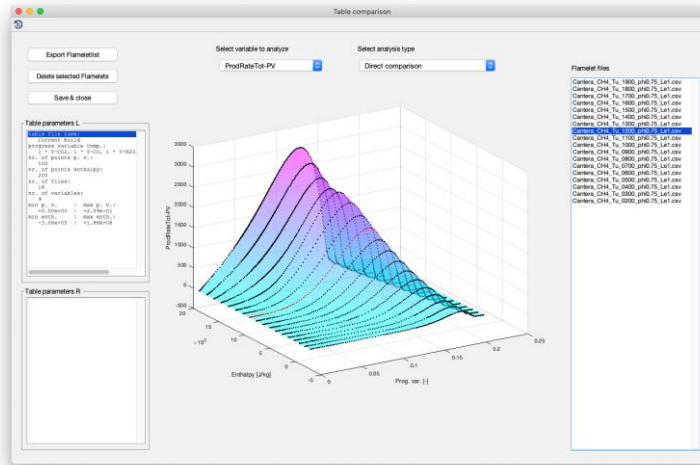
1. Perform 1D simulations (detailed chemistry)

- Open source solvers:
 - Cantera for steady state simulations
 - Ember for transient flame calculations



2. Tabulate 1D solutions in look-up tables

- ▶ Tabulate as $f(\text{progress var.}, \text{enthalpy})$
- ▶ In house developed tool
- ▶ Cantera, Ember, and FlameMaster^[5] support



3. Solve 3D transport equations

- ▶ Just additional 4 PDEs, reaction source terms from look-up tables

The SUZ logo, featuring the letters 'SUZ' in a bold, sans-serif font. The 'S' and 'Z' are red, and the 'U' is blue.

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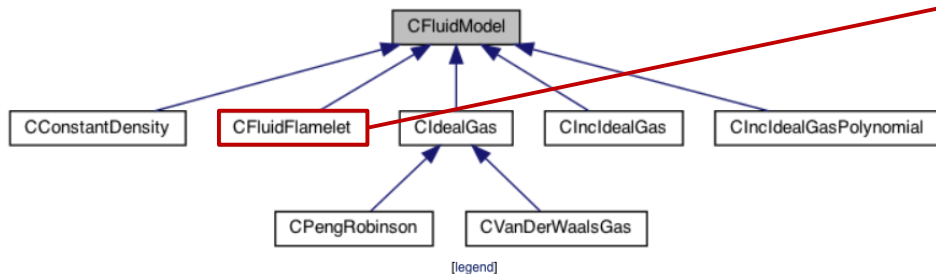
OUTLOOK

Implementation in SU2

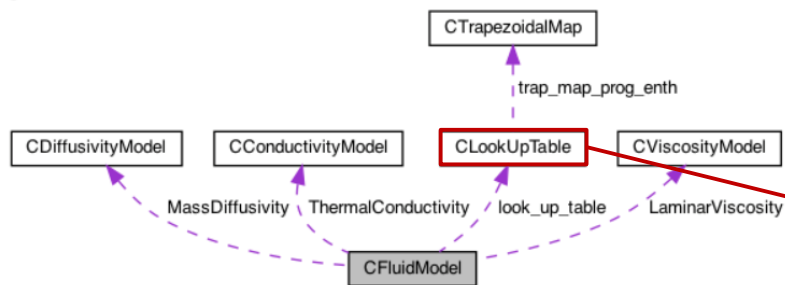
Architecture

https://github.com/su2code/SU2/tree/feature_flamelet

Inheritance diagram for CFluidModel:



Collaboration diagram for CFluidModel:



CFluidFlamelet

Public Member Functions

```
CFluidFlamelet (CConfig *config, su2double value_pressure_operating)
~CFluidFlamelet ()
unsigned long SetTDSState_T (su2double val_temperature, su2double *val_scalars)
Virtual member. More...
unsigned long GetEnthFromTemp (su2double *enthalpy, su2double val_prog, su2double val_temp)
CLookUpTable * GetLookUpTable ()
su2double GetMassDiffusivity ()
Get fluid mass diffusivity. More...
su2double GetThermalConductivity ()
Get fluid thermal conductivity. More...
su2double GetLaminarViscosity ()
Get fluid dynamic viscosity. More...
pair< su2double, su2double > GetTableLimitsEnth ()
pair< su2double, su2double > GetTableLimitsProg ()
su2double GetdDensitydPV ()
su2double GetdSourcePVdPV ()
su2double GetdDensitydEnth ()
```

CLookUpTable [6]

Public Member Functions

```
CLookUpTable (string file_name_lut)
void PrintTableInfo ()
unsigned long LookUp_ProgEnth (string val_name_var, su2double *val_var, su2double val_prog, su2double val_enth)
unsigned long LookUp_ProgEnth (vector< string > &val_names_var, vector< su2double * > &val_vars, su2double val_prog, su2double val_enth)
pair< su2double, su2double > GetTableLimitsEnth ()
pair< su2double, su2double > GetTableLimitsProg ()
```

- A dark blue arrow is used to visualize a public inheritance relation between two classes.

- A purple dashed arrow is used if a class is contained or used by another class. The arrow is labelled with the variable(s) through which the pointed class or struct is accessible.

Implementation in SU2

Configuration

https://github.com/su2code/SU2/tree/feature_flamelet

- ▶ Implemented in incompressible solver [7]
- ▶ Arbitrary number of scalar transport equations $(h, C, Y_1, Y_2, \dots, Y_N)$
 - ▶ `config.cfg`: `SCALAR_NAMES= (Enthalpy, ProgVar, Y-CO, Y-NO)`
 - ▶ Total enthalpy and progress variable must always be the first and second transported variable
- ▶ Handling of source terms:

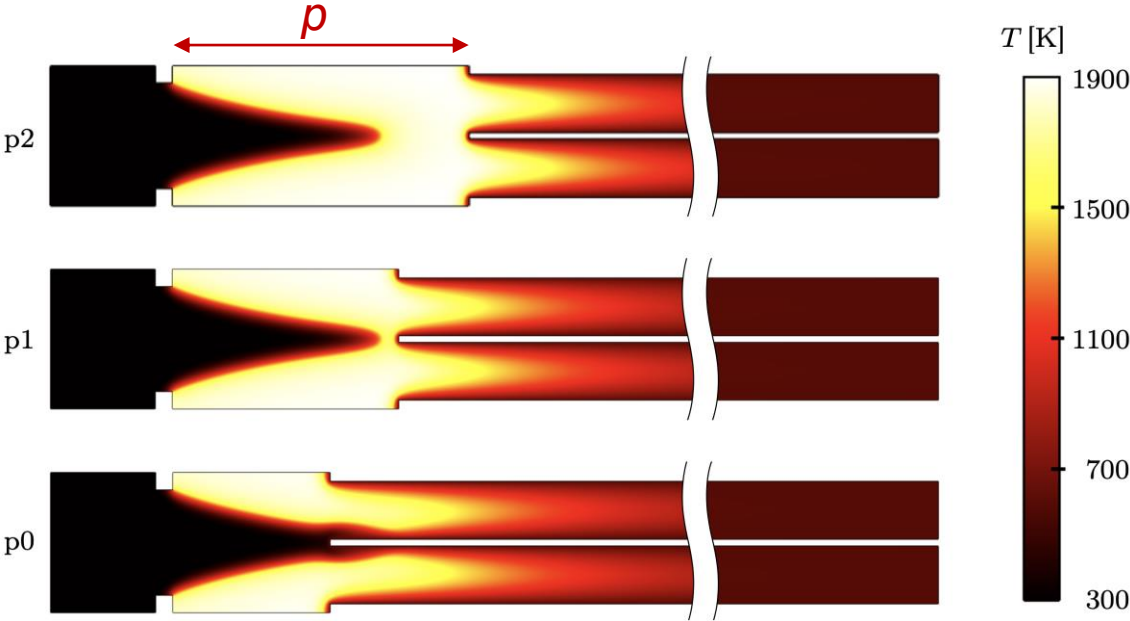
	<u>src enth.</u>	<u>src p.v.</u>	<u>src Y-CO</u>	<u>src Y-NO</u>
▶ <code>config.cfg</code> : <code>SCALAR_SOURCETERM_NAMES=</code>	<code>(NULL, NULL,</code>	<code>S-PV, NULL,</code>	<code>Spos-CO, Sneg-CO,</code>	<code>Spos-NO, Sneg-NO)</code>

 - ▶ Names of source terms must correspond to names in the lookup table
 - ▶ Names can be NULL for no source term: reduces to transport of passive scalar
- ▶ Non-transported lookup variables (looked up for visualization)
 - ▶ `config.cfg`: `LOOKUP_NAMES=(Src-PV, MolarWeightMixture, Y-CO-TABLE)`
- ▶ Lookup table: ASCII file with unstructured data
 - ▶ `config.cfg`: `FILENAME_LUT = chemtable.drg`

Implementation in SU2

Model validation

Test case for validation / verification



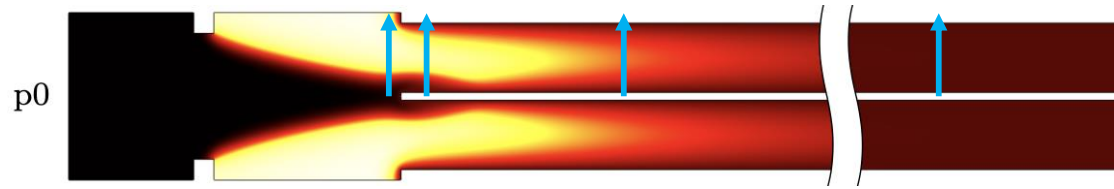
Investigated operating points

	$p = 4.5 \text{ mm}$	$p = 6.5 \text{ mm}$	$p = 8.5 \text{ mm}$
Adiabatic wall	p0.adia	p1.adia	p2.adia
$T_{\text{wall}} = 1800 \text{ K}$	p0.1800	p1.1800	p2.1800
$T_{\text{wall}} = 1500 \text{ K}$	p0.1500	p1.1500	p2.1500
$T_{\text{wall}} = 1200 \text{ K}$	p0.1200	p1.1200	p2.1200
$T_{\text{wall}} = 900 \text{ K}$	p0.0900	p1.0900	p2.0900
$T_{\text{wall}} = 600 \text{ K}$	p0.0600	p1.0600	p2.0600
$T_{\text{wall}} = 300 \text{ K}$	p0.0300	p1.0300	p2.0300

Validation data generated with detailed chemistry CFD code CIAO [8]

Implementation in SU2

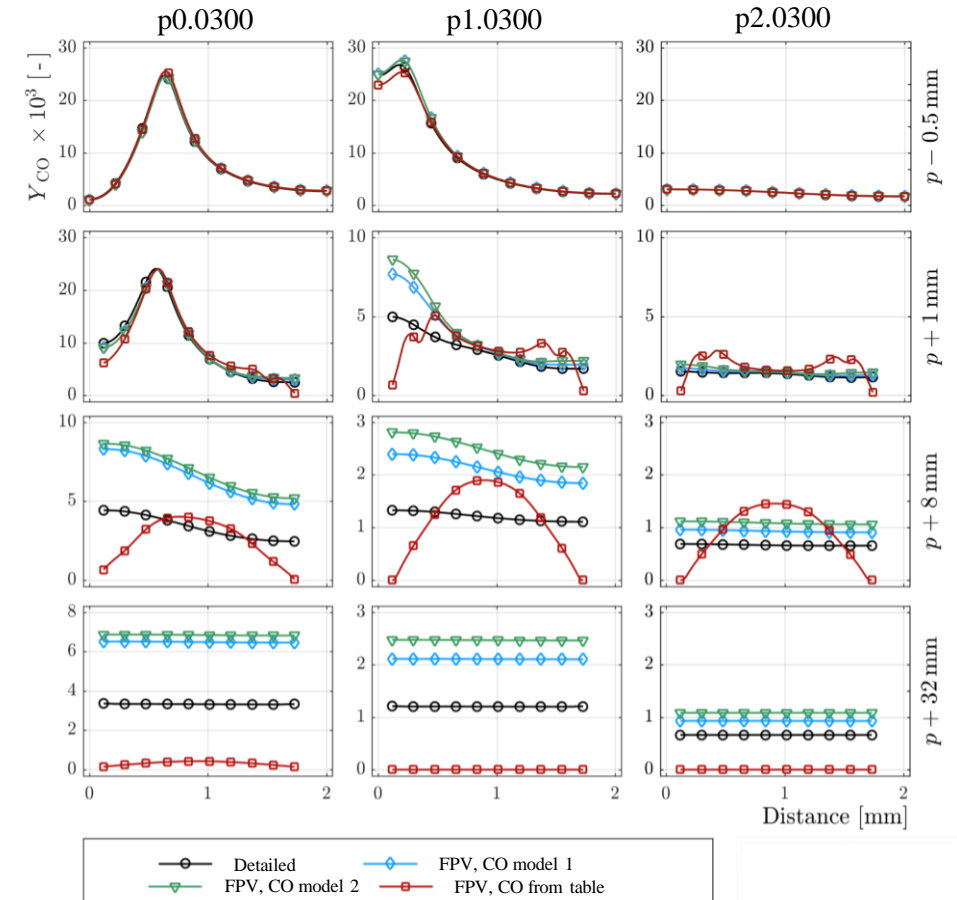
Model validation



Blue arrows: plot lines in figure on the right

- ▶ 3 models with different computational costs investigated
- ▶ Table look-up (red) is not physically correct
- ▶ Model 1 (blue) shows best agreement but expensive
- ▶ Model 2 (green) shows best accuracy/cost trade-off

Model used in this work



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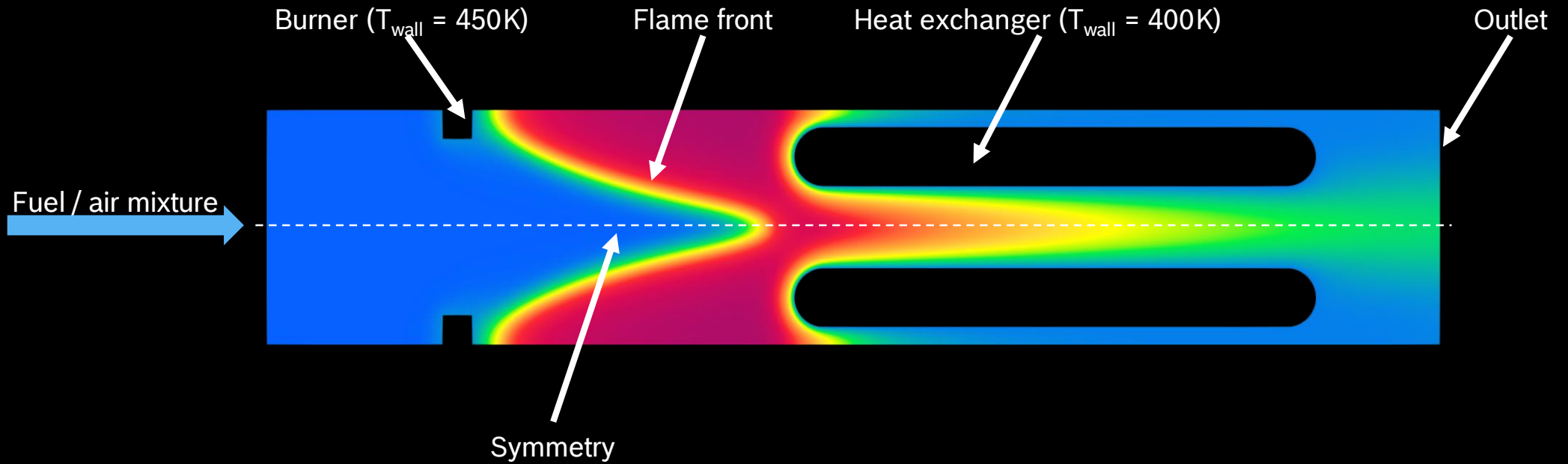
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OUTLOOK

Application to Optimization

Case setup

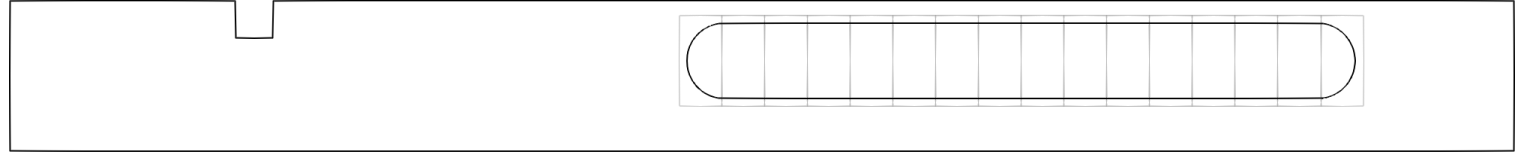


Goal: Shape optimization of heat exchanger geometry to reduce Y_{CO} , Y_{NO} , & Temperature

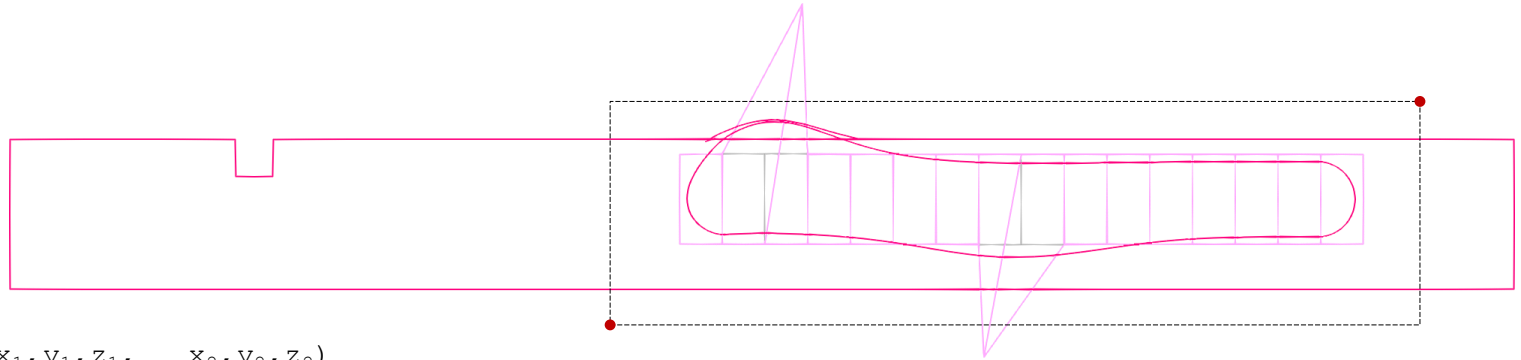
Application to Optimization

Geometrical deformation constraints

Original geometry and FFD box

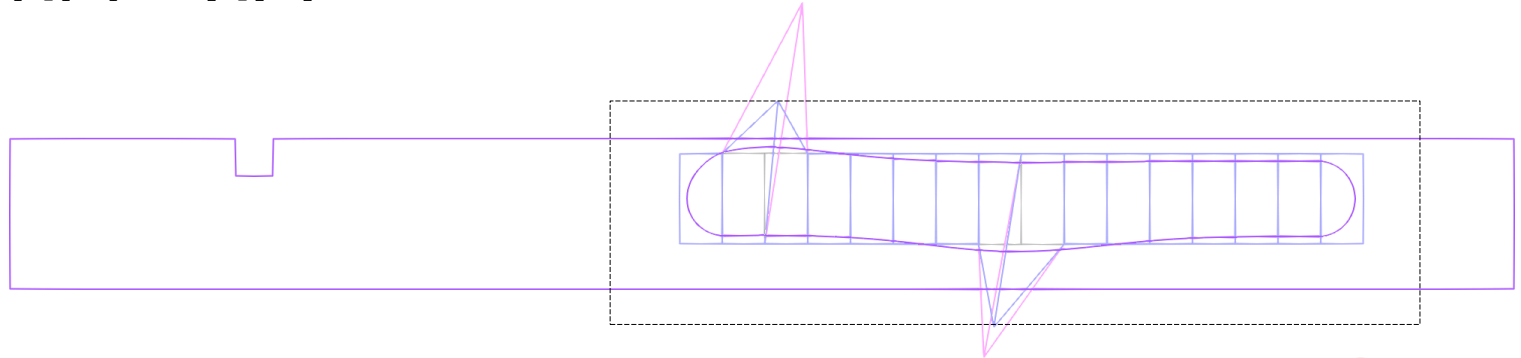


Deformed geometry and FFD box without constraints



config.cfg: FFD_BOUNDS = (<FFD BOX ID>, x_1, y_1, z_1 , x_2, y_2, z_2)

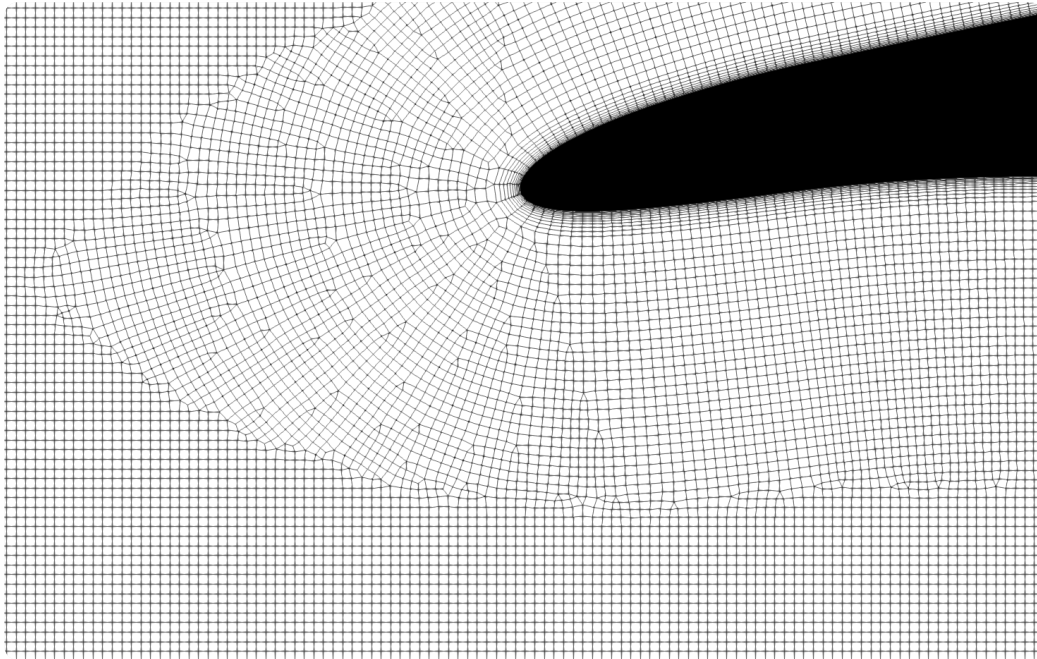
Deformed geometry and FFD box with constraints



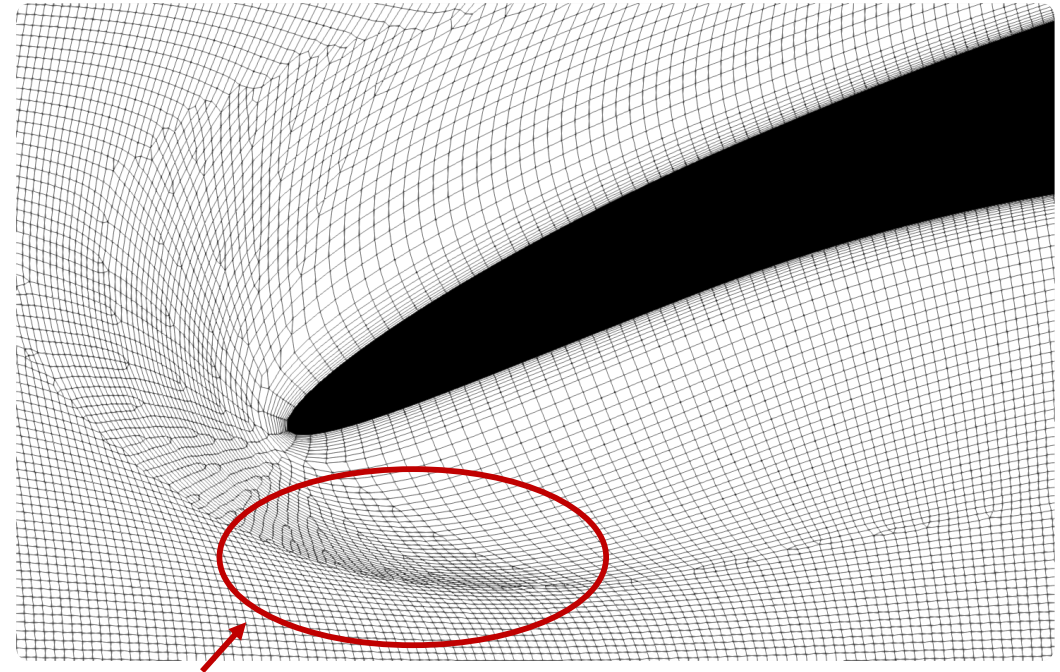
Application to Optimization

Large mesh deformation may result in low mesh quality

Before deformation



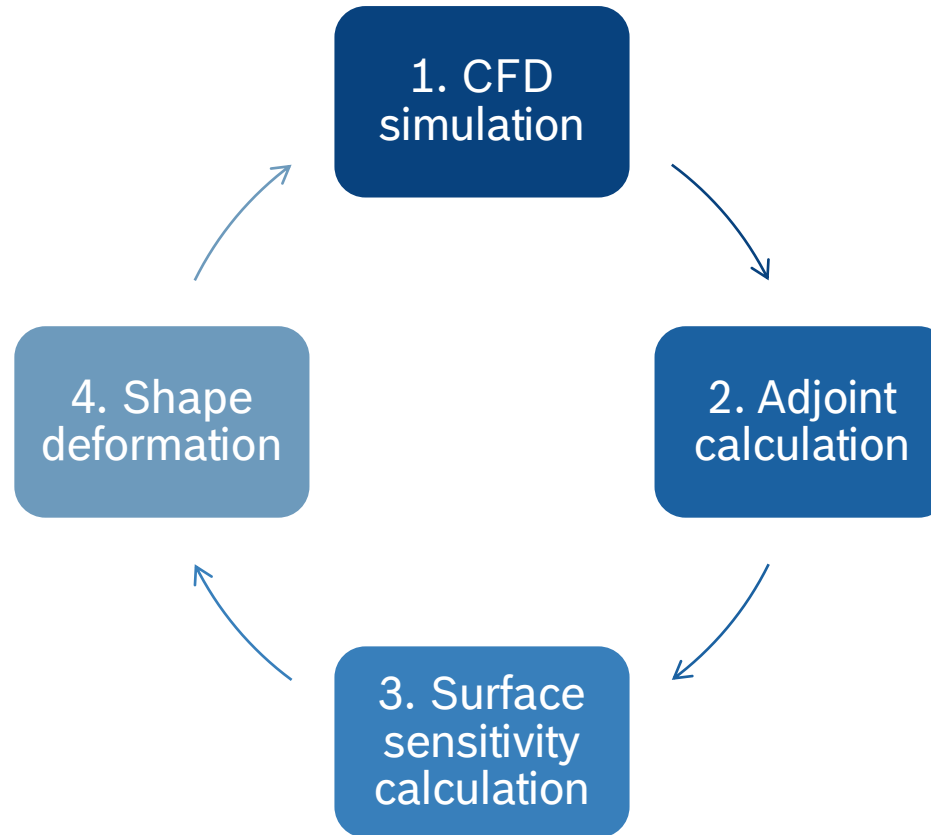
After deformation



That's bad.

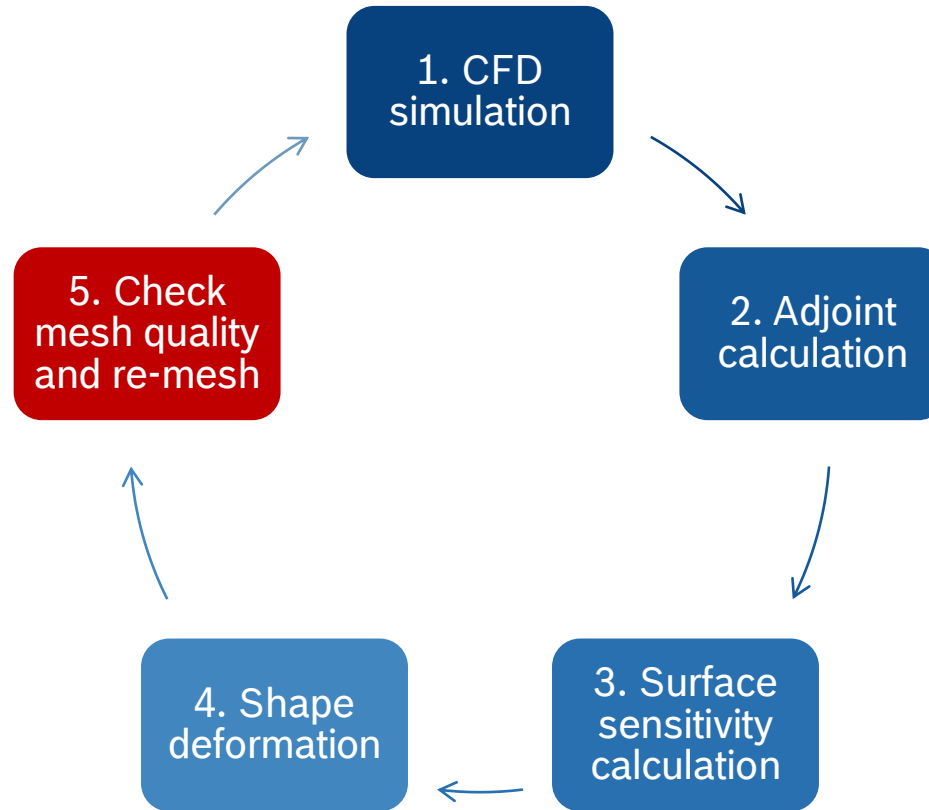
Application to Optimization

Solution: Automated Remeshing



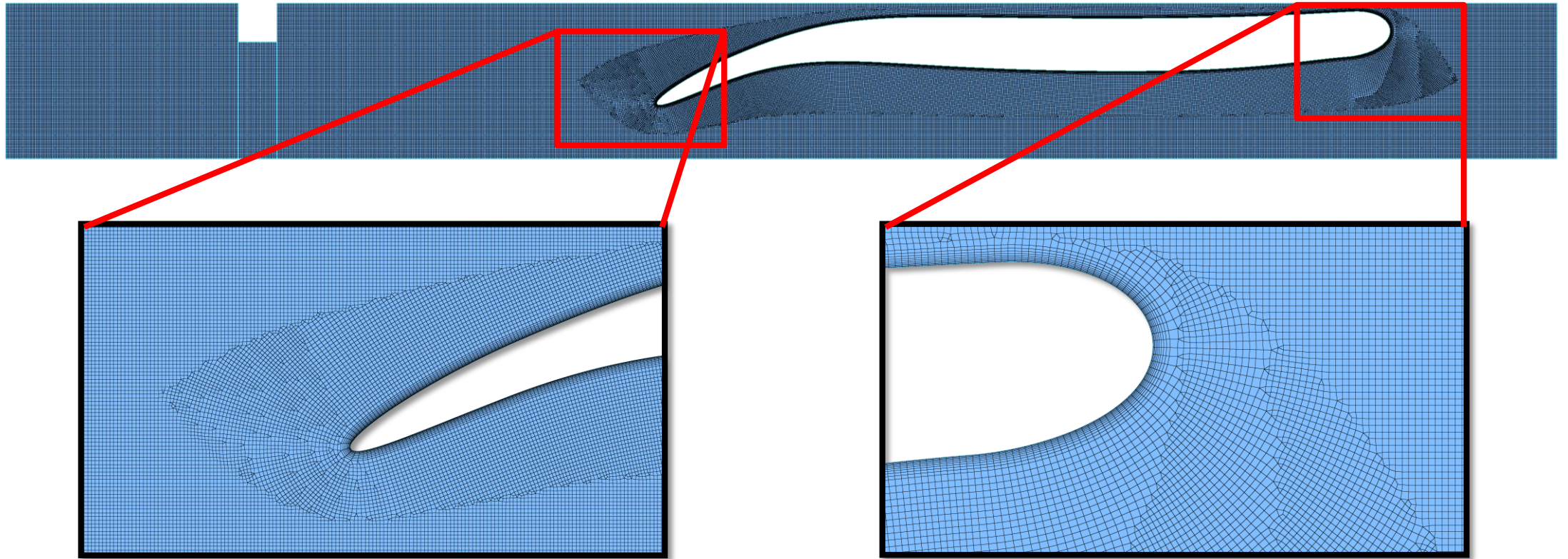
Application to Optimization

Solution: Automated Remeshing



Application to Optimization

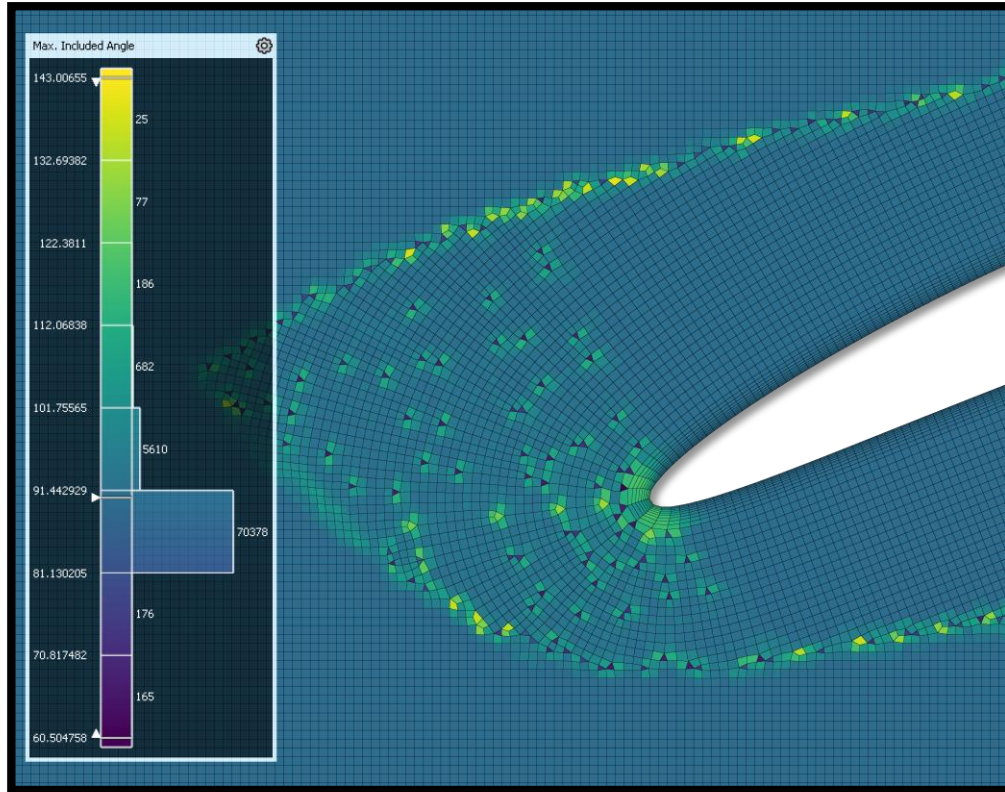
Baseline Grid



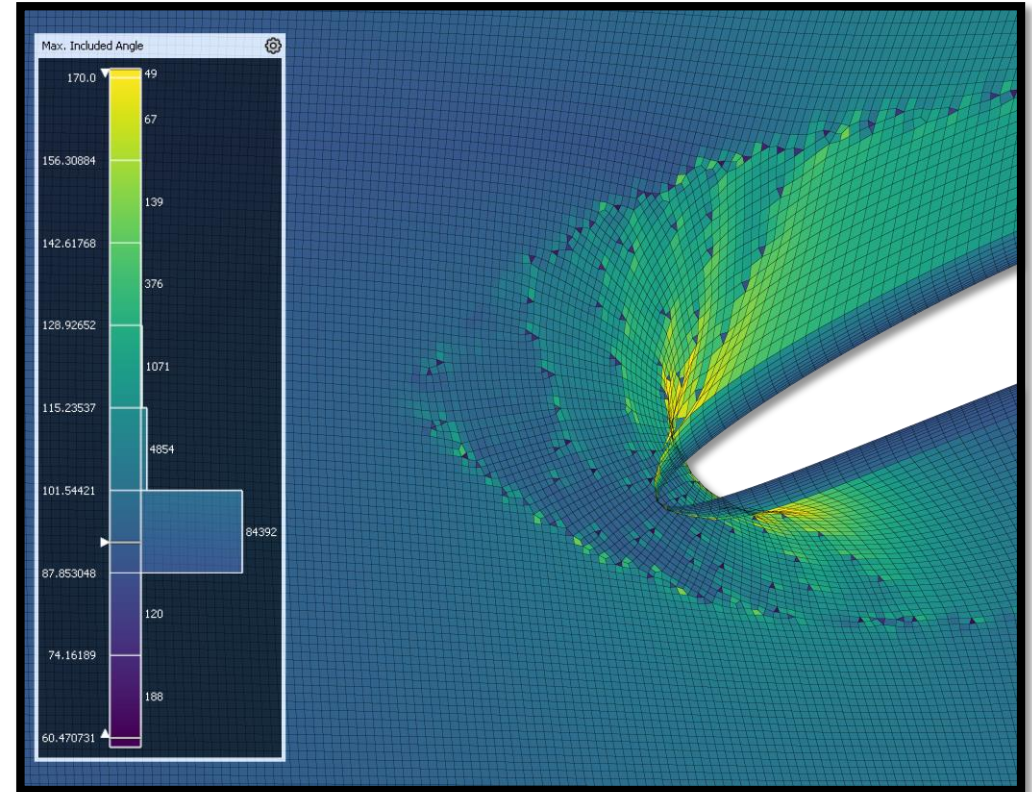
**Hybrid quad-dominant grid generated using
Pointwise**

Application to Optimization

Grid Quality Investigation



Max. Angle < 170 deg.



Max. Angle > 170 deg.

Application to Optimization

Automatic Remeshing

```
package require PWI_Glyph

# User parameters
set filename "mesh_03_deformed_neg_vol_updated"
set quality 170
set interiorEdgeName "wall_probe"
set probeSpacing 2e-5

# Procedure to remove entities from a list
proc lremove {listVariable value} {
    set idx [lsearch -exact $listVariable $value]
    return [lreplace $listVariable $idx $idx]
}

# Load the defaults
set cwd [file dirname [info script]]
pw::Application load "$cwd/Defaults.pw"

# Import the SU2 grid file
set importMode [pw::Application begin GridImport]
$importMode initialize -strict -type SU2 "$cwd/$filename.su2"
$importMode setAttribute GridImportConditionData true
$importMode read
$importMode convert
$importMode end

set domains [pw::Grid getAll -type pw::Domain]
set connectors [pw::Grid getAll -type pw::Connector]

# Examine grid quality
set examine [pw::Examine create DomainMaximumAngle]
$examine addEntity $domains
$examine examine
set max [$examine getMaximum]

puts "Max. Angle = $max deg."

if {$max > $quality} {
    puts "Quality lower than re-meshing threshold."
    puts "Begin re-meshing operation."
} else {
    puts "Quality higher than re-meshing threshold."
    puts "Exiting."
    exit
}
```



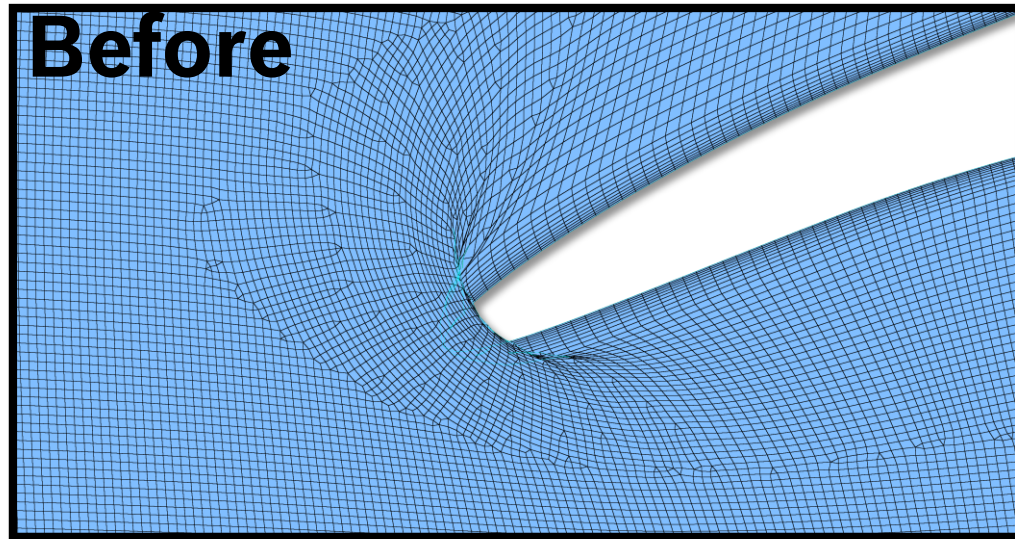
config.cfg:

```
ENABLE_REMESHING = YES
```

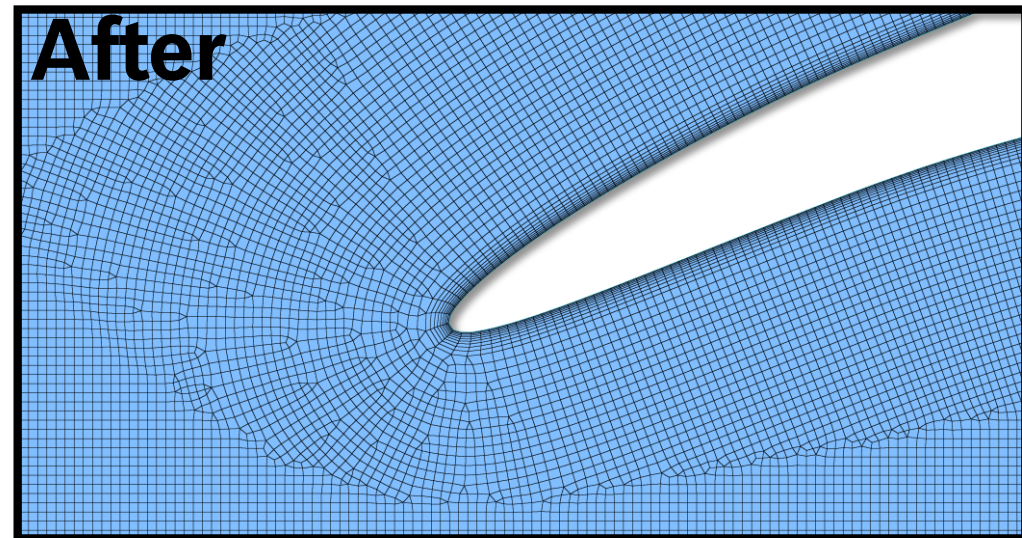
Provide files:

```
pointwise_defaults.pw
pointwise_remesh.glf
```

Before



After



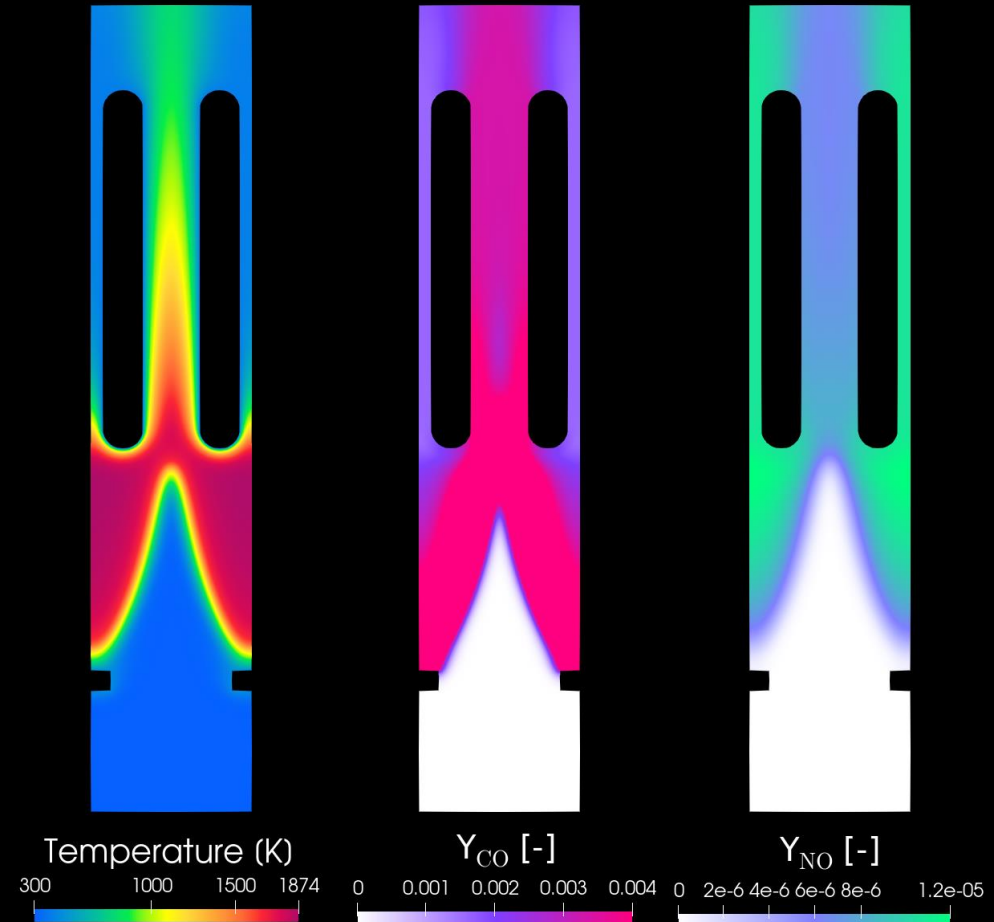
Application to Optimization

Results

5 optimizations were performed with the following objective weights:

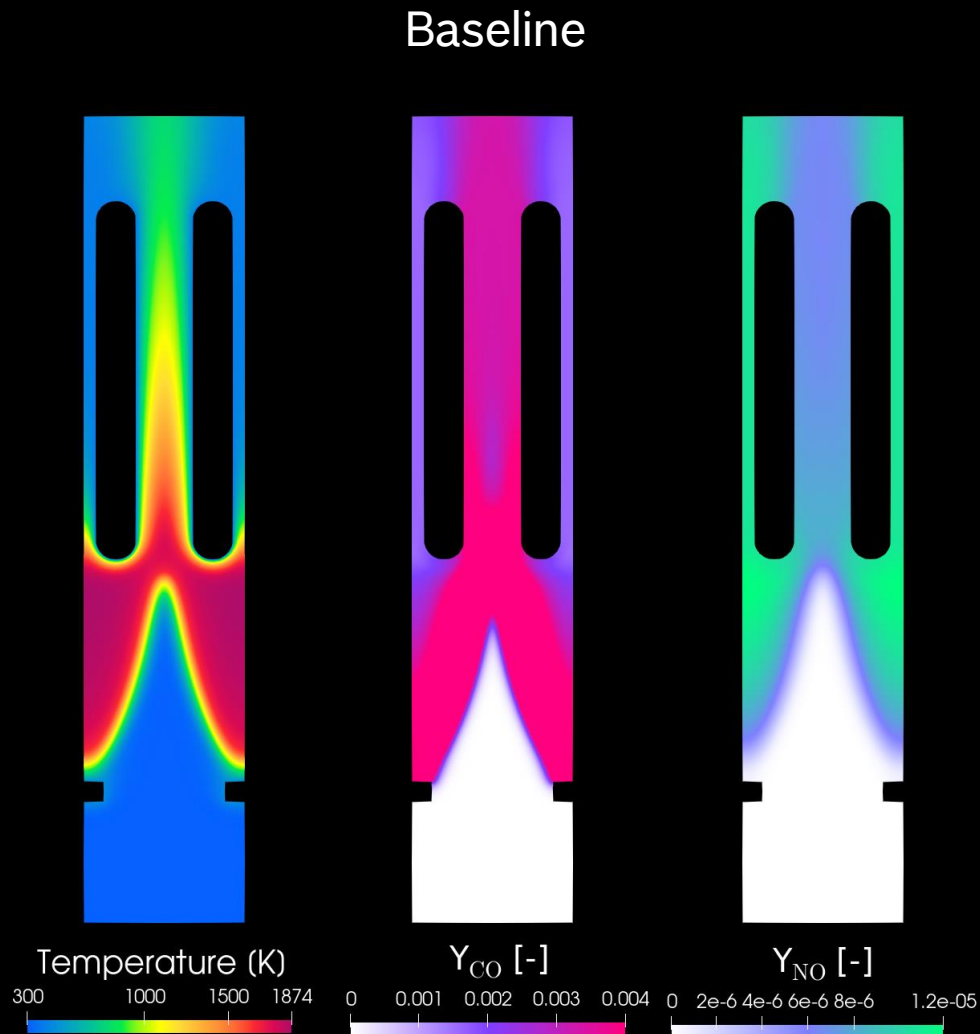
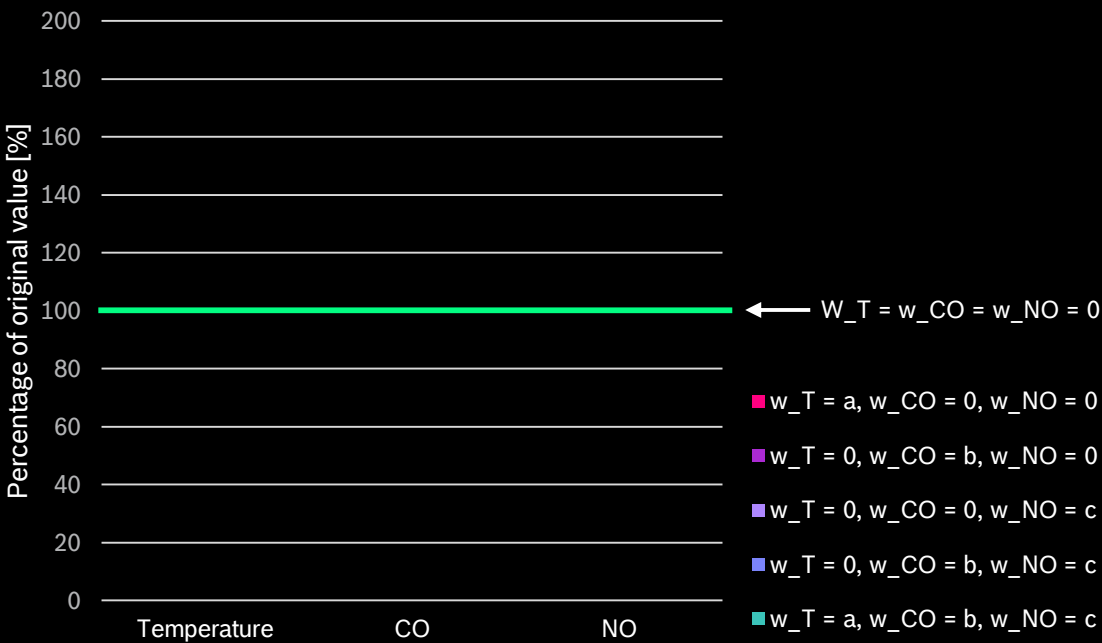
T	Y_{CO}	Y_{NO}
$5e-10=a$	0	0
0	$1e-4=b$	0
0	0	$1e-2=c$
0	$1e-4=b$	$1e-2=c$
$5e-10=a$	$1e-4=b$	$1e-2=c$

Baseline



Application to Optimization

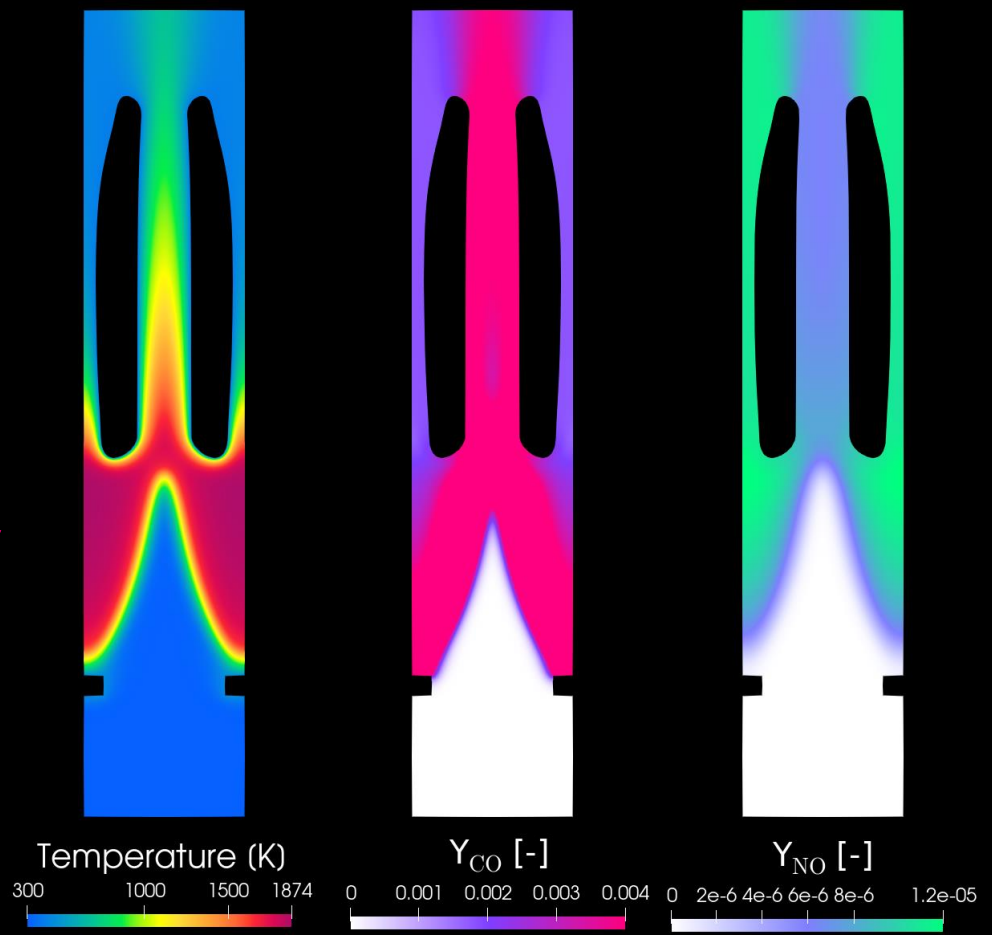
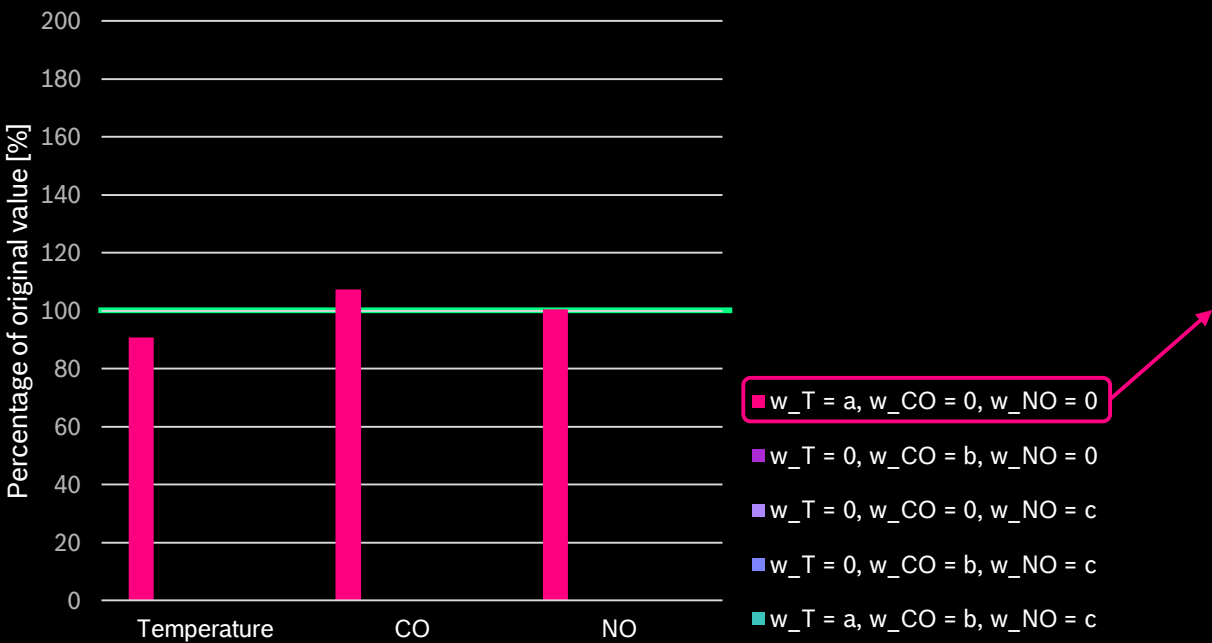
Results



Application to Optimization

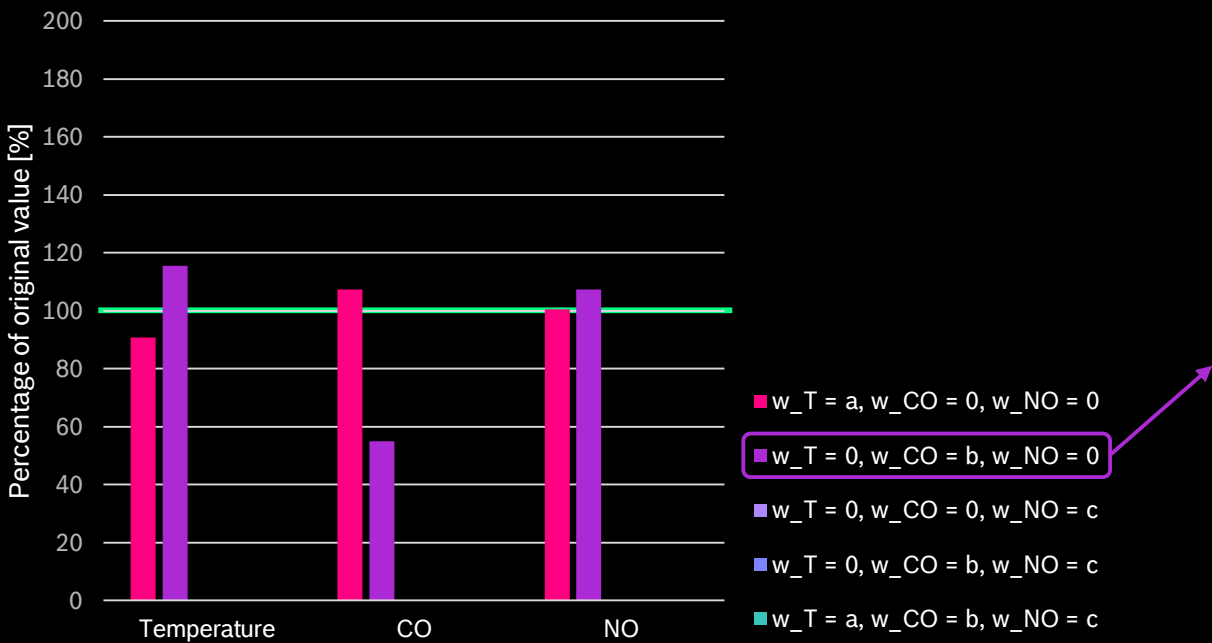
Results

Optimize Temperature only

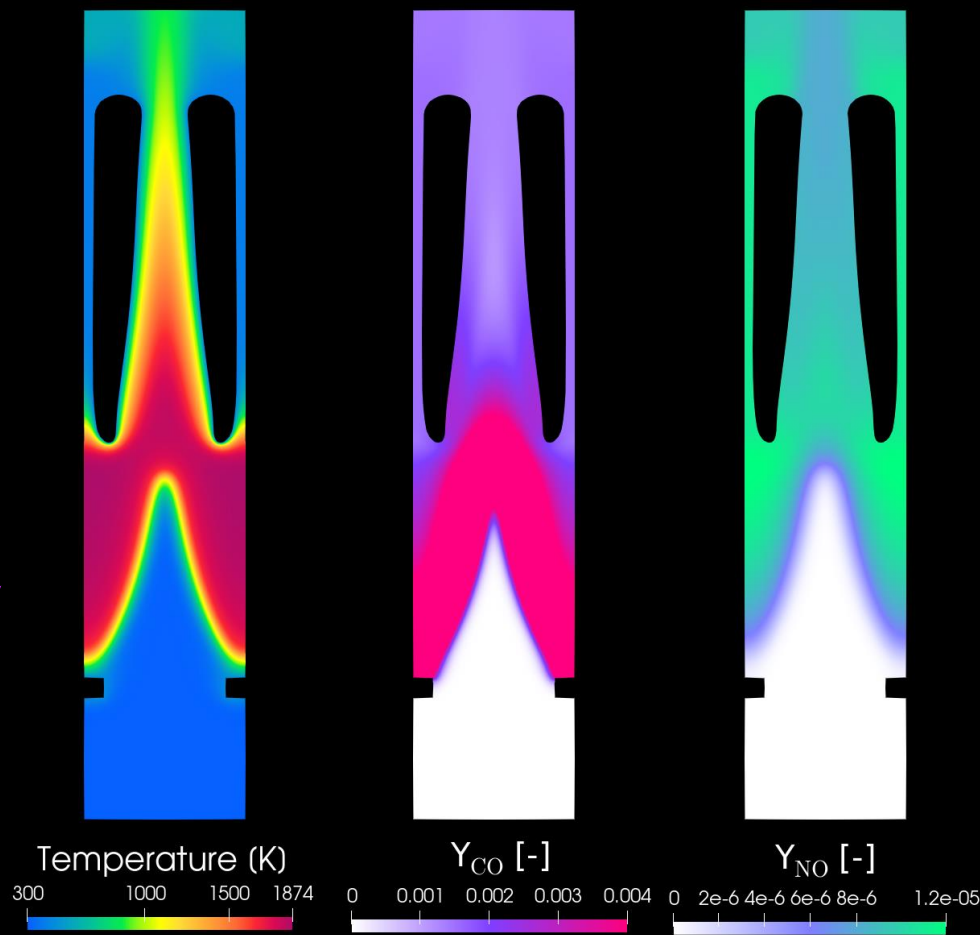


Application to Optimization

Results



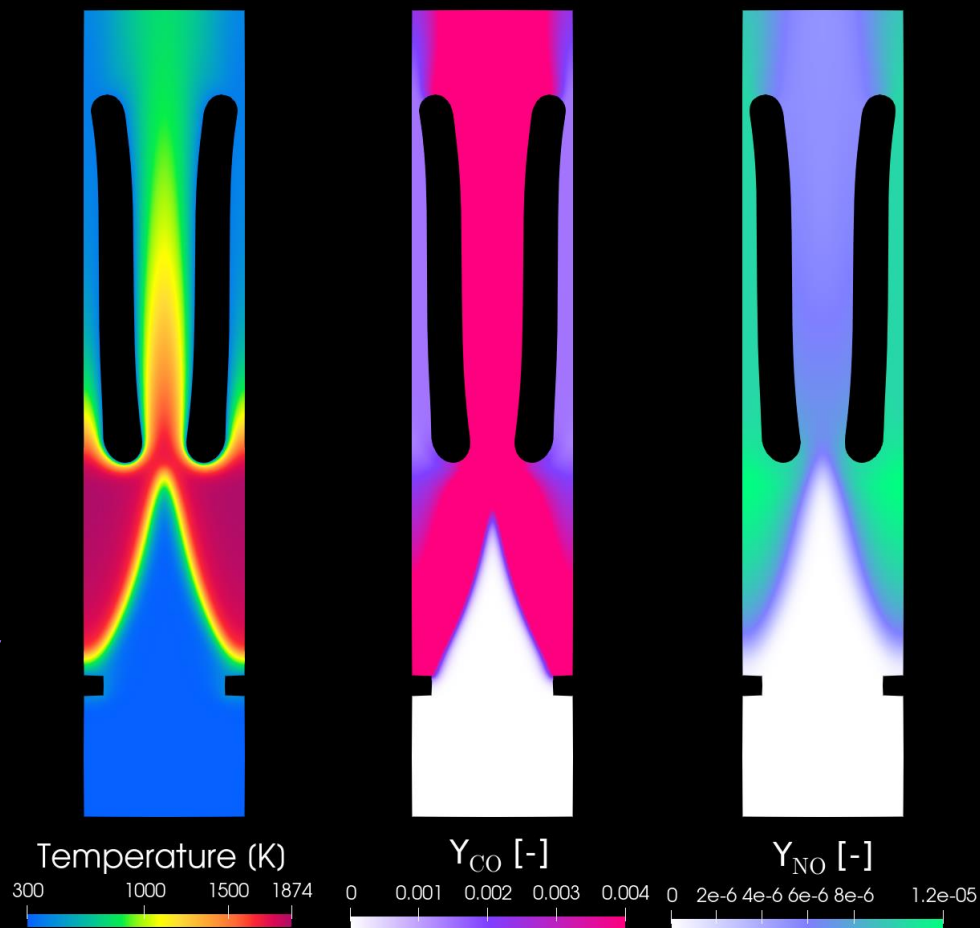
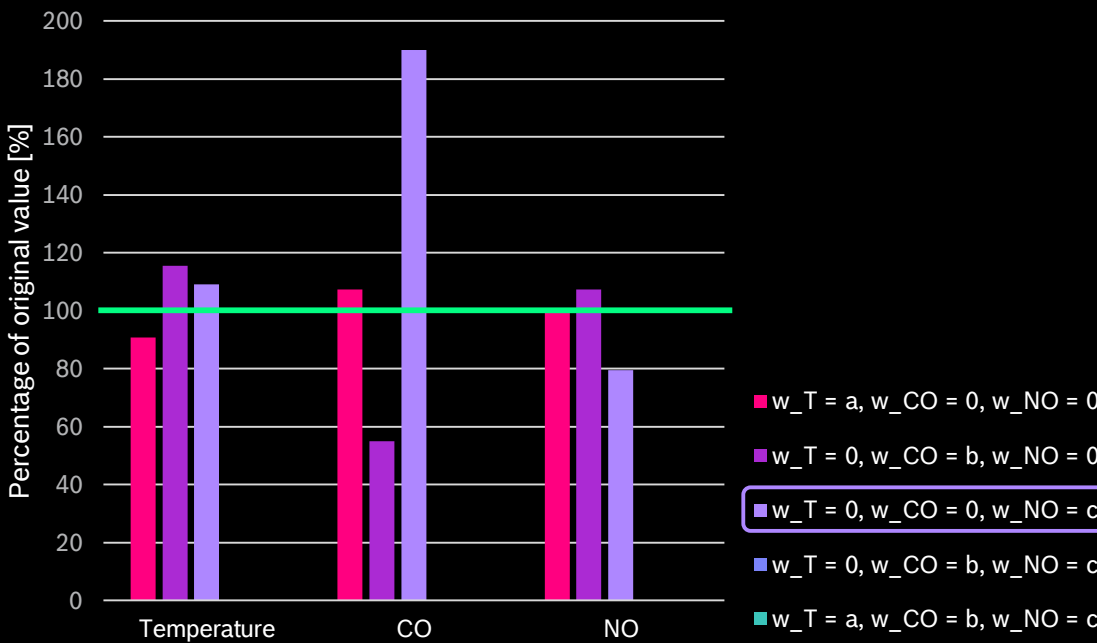
Optimize Y_{CO} only



Application to Optimization

Results

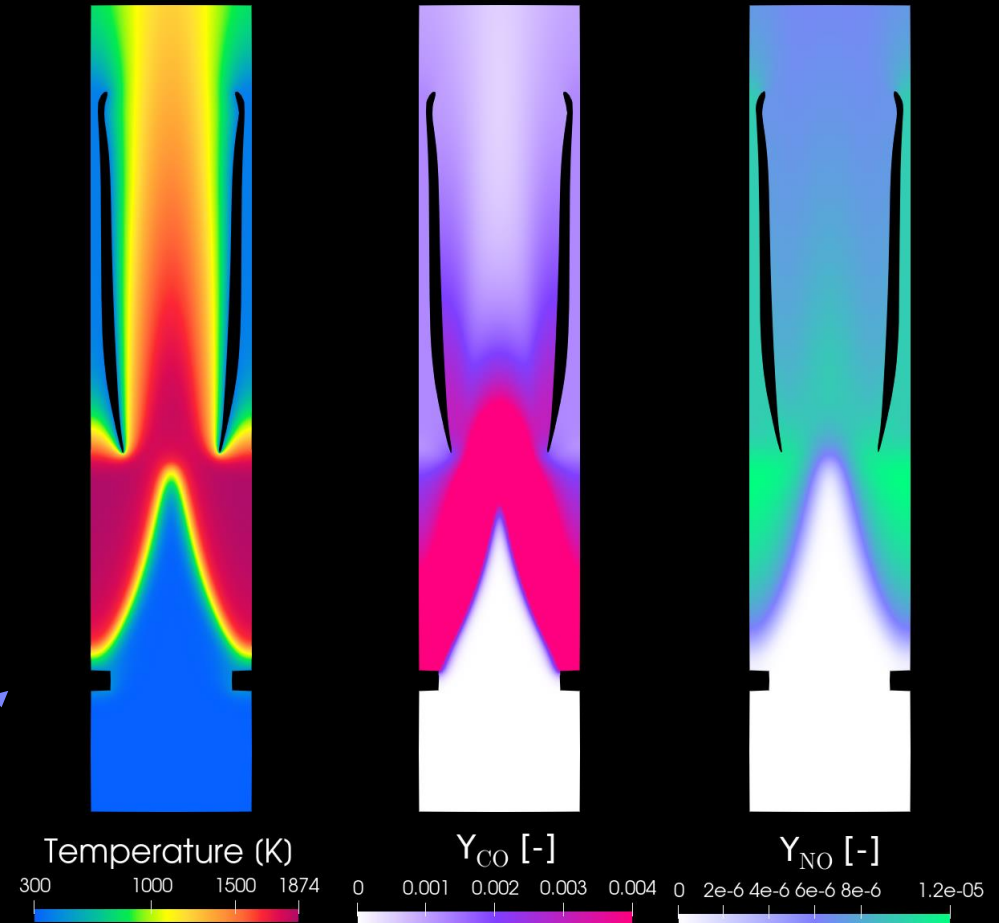
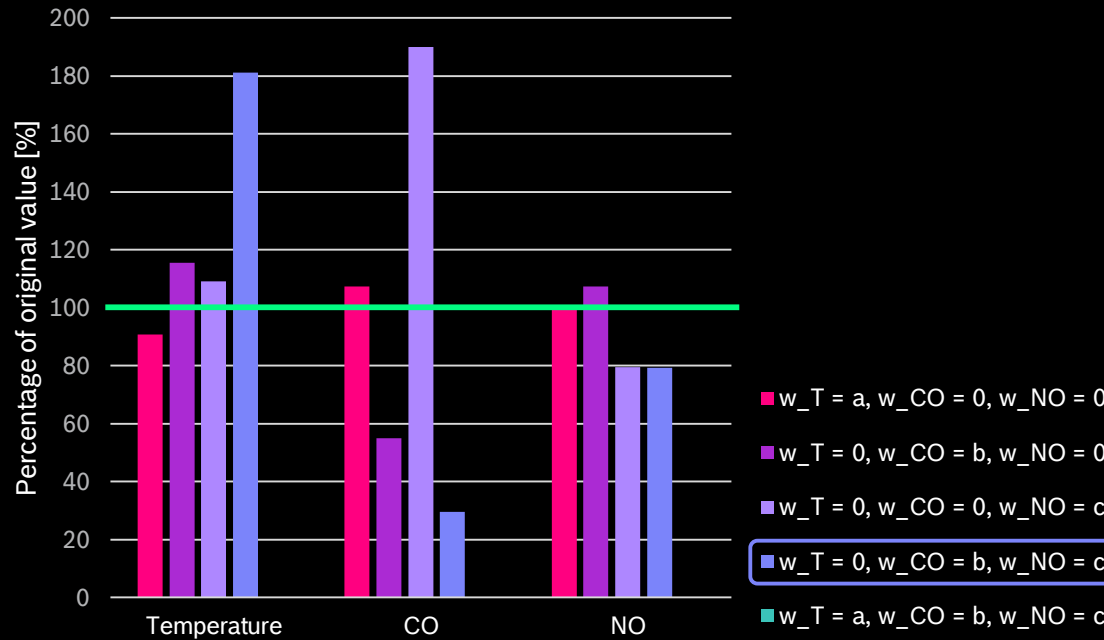
Optimize Y_{NO} only



Application to Optimization

Results

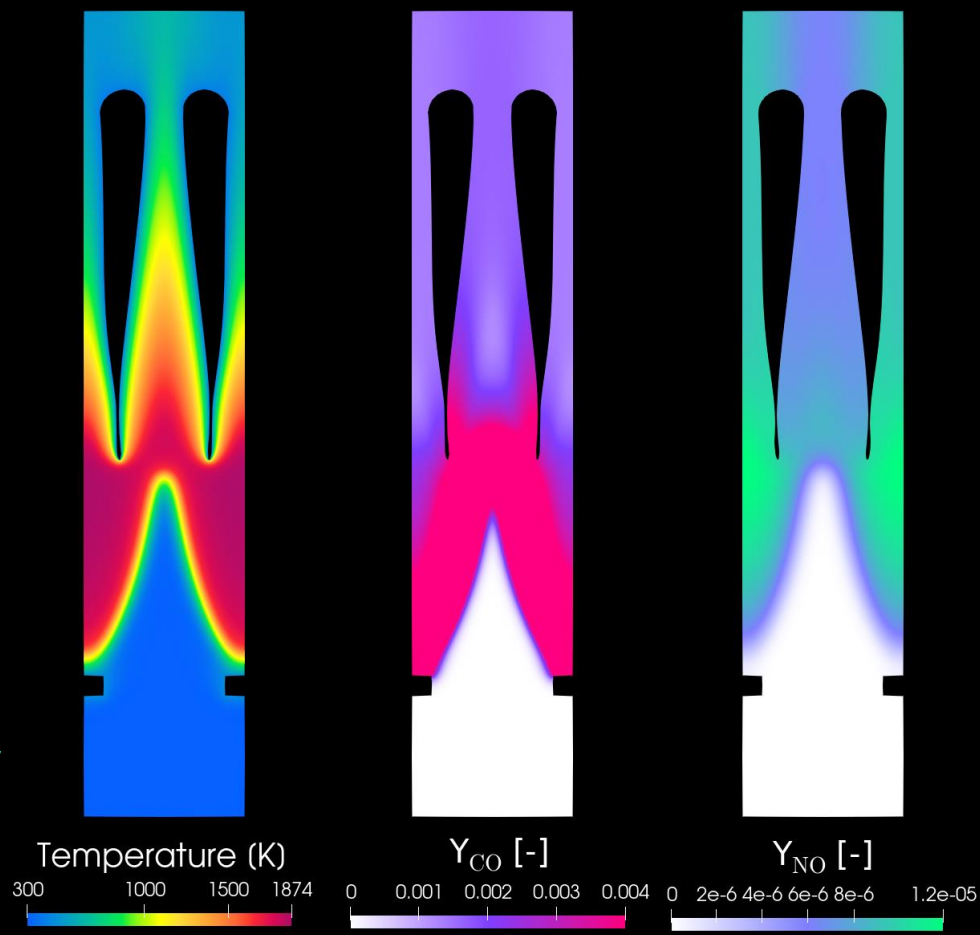
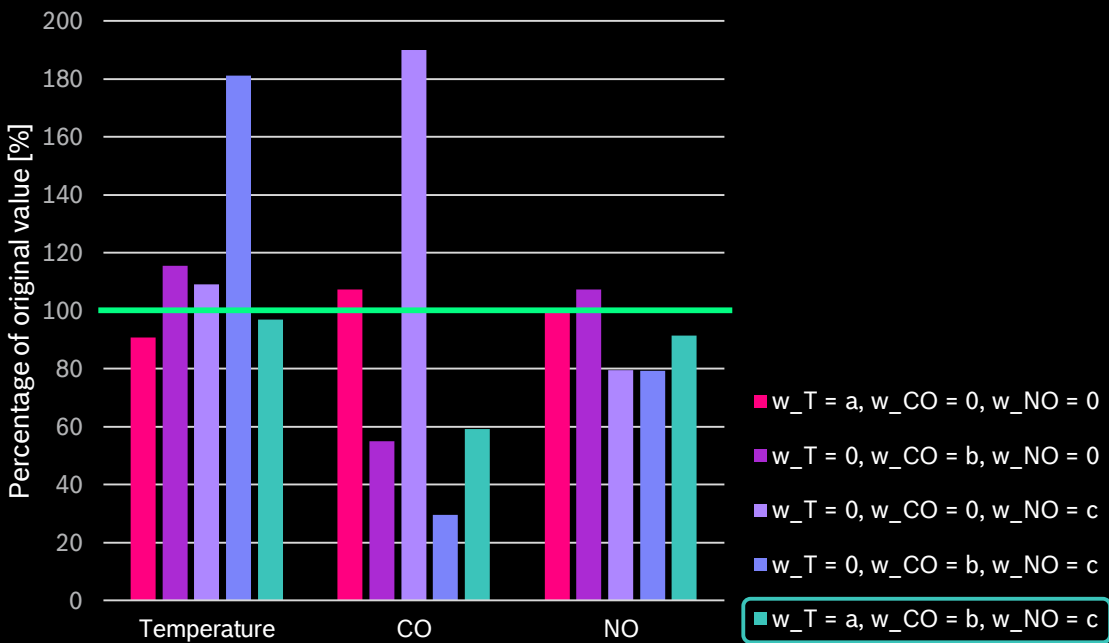
Optimize Y_{CO} & Y_{NO}



Application to Optimization

Results

Optimize Y_{CO} , Y_{NO} , and Temperature



Application to Optimization Results

Optimization objectives:

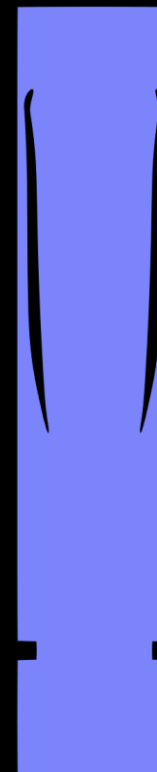
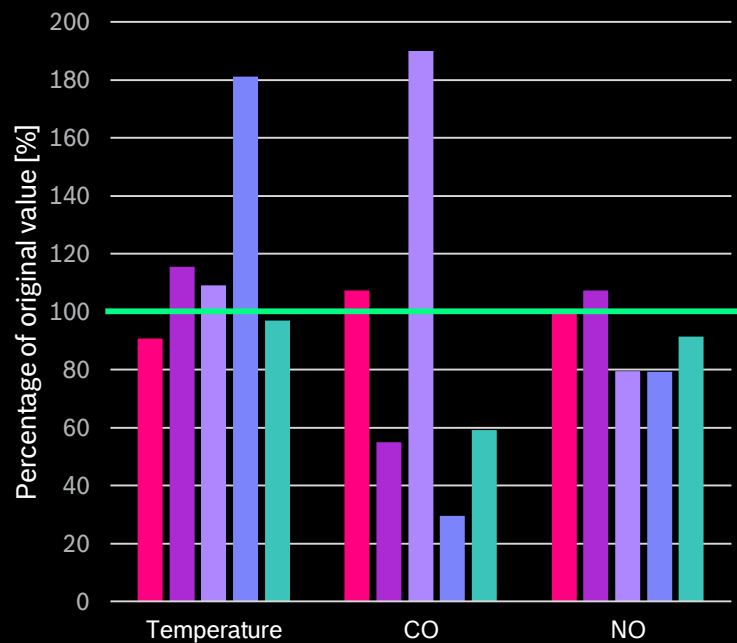
T

Y_{CO}

Y_{NO}

Y_{CO}, Y_{NO}

Y_{CO}, Y_{NO}, T



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OUTLOOK

Implementation of more sophisticated geometrical constraints

Application to more realistic 3D heat exchanger geometry

Inclusion of conjugate heat transfer model

Hydrogen combustion → partially premixed flames, 3D lookup tables

THANK YOU